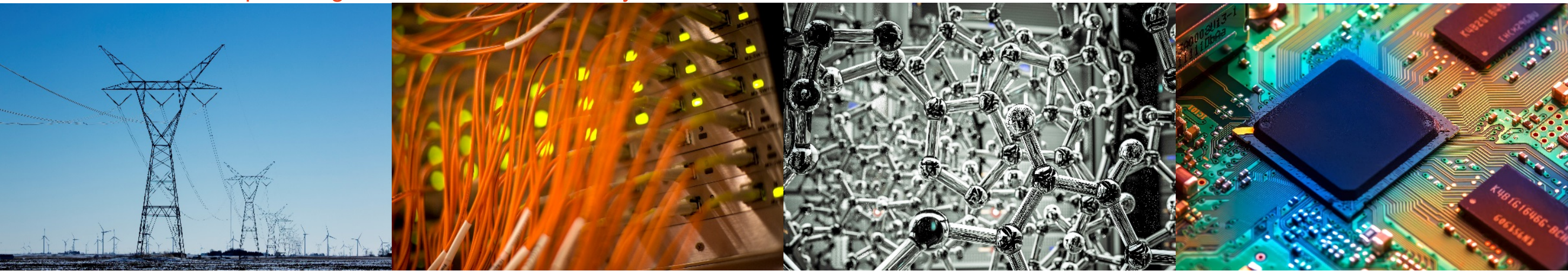


The role of molecular ions in the overall ionic composition of polar wind outflow

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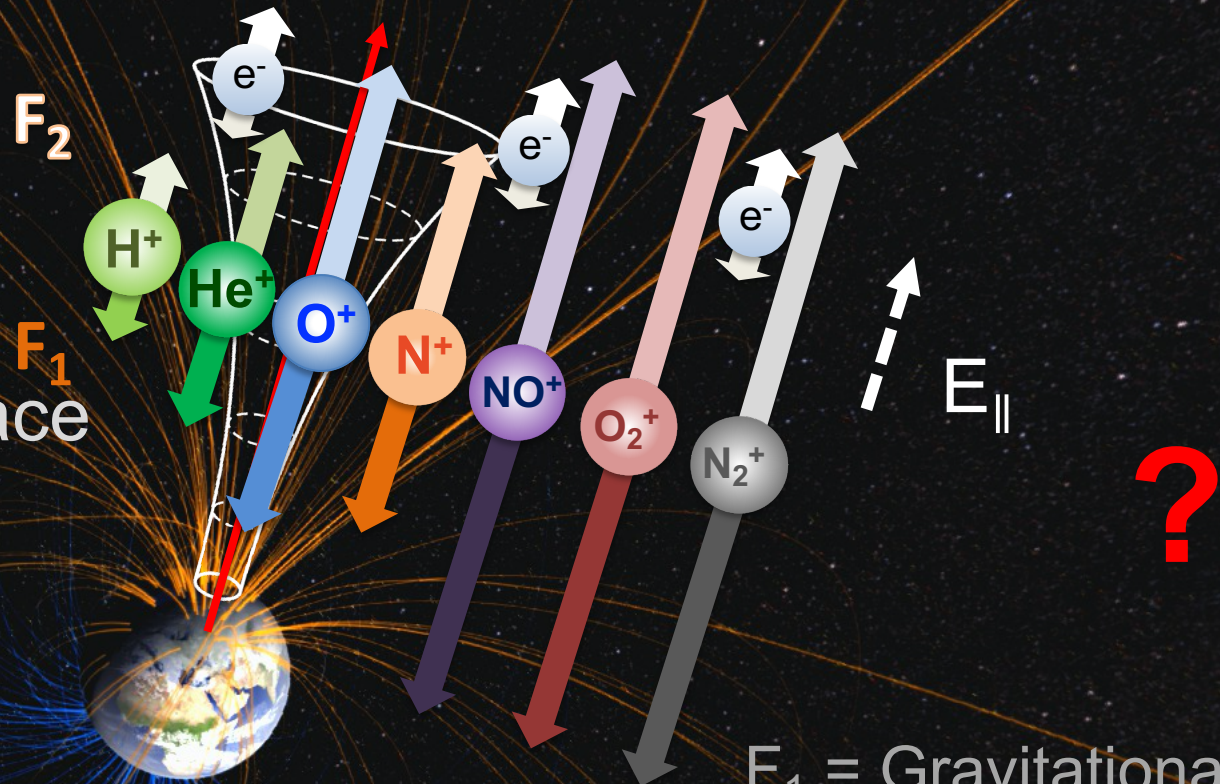


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Ions and electrons escape via open field lines to the Earth's magnetosphere and to outer space

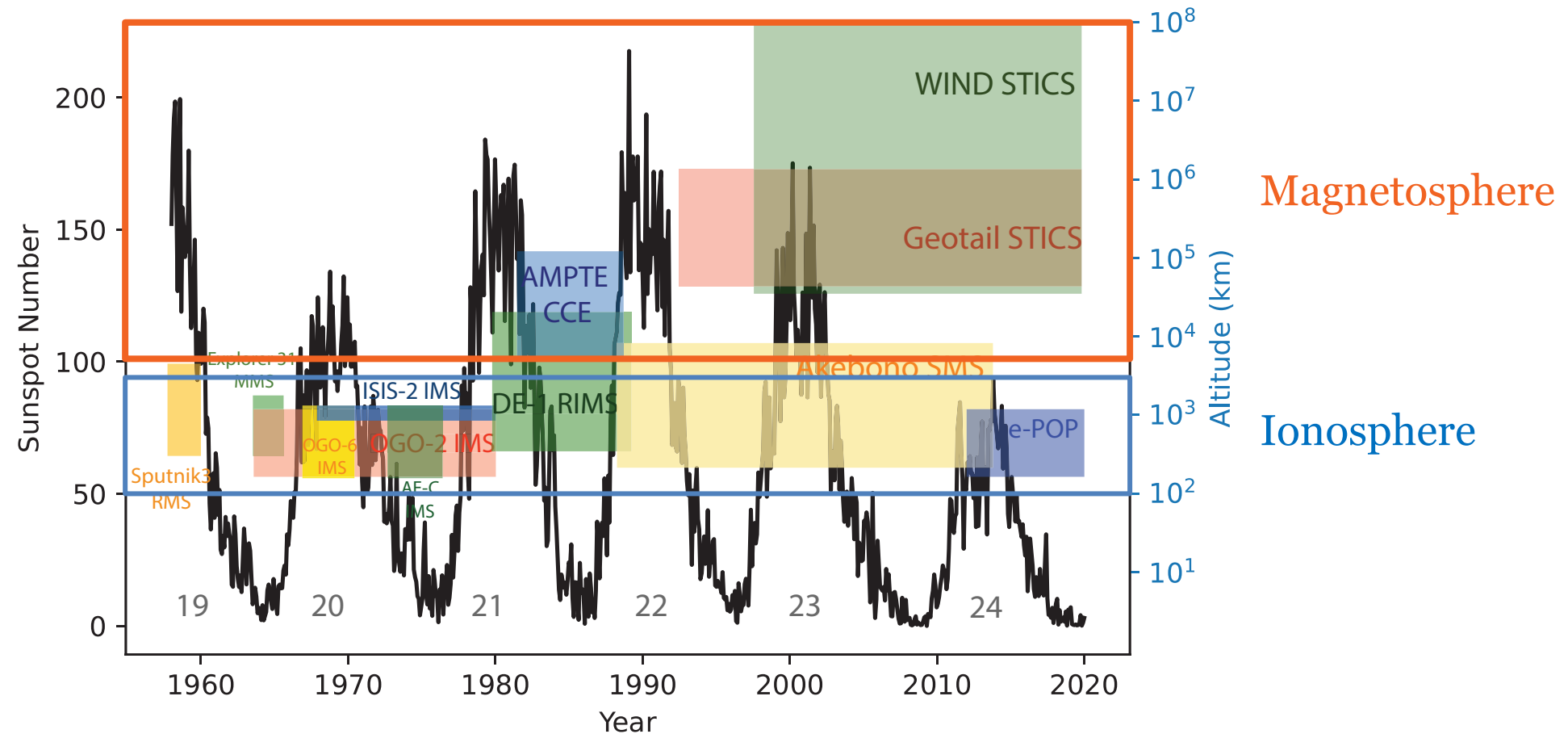


$F_1 = \text{Gravitational}$
 $F_2 = \text{Electromagnetic}$

$$E = \frac{1}{2}mv^2 - \frac{gMm}{r}$$

Escape:
 $E_{\text{esc}}(e^-) \geq 0.7 \text{ eV}$
 $E_{\text{esc}}(\text{Ions}) \geq 10 \text{ eV}$

60 Years of N⁺ observation



- The presence of N⁺ ions could change plasma characteristics in the inner magnetosphere.

Polar Wind Outflow Model (referred to as **3iPWOM**)

- Chemical & Collisional Scheme
- Suprathermal Electron: GLOW
- Neutral Density: NRLMSISE-90

At each time step, solves for the n , T , v , and E_{\parallel}

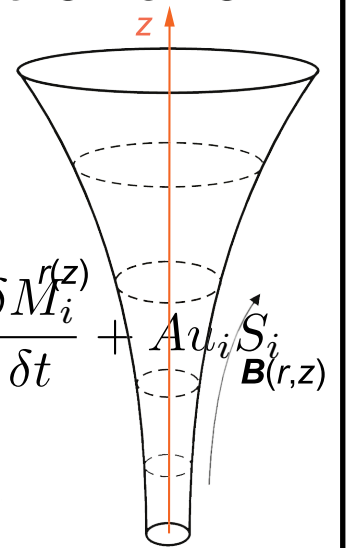
Solves for the **transport** and E_{\parallel} equations for H^+ , He^+ , O^+

$$\frac{\partial}{\partial t}(A\rho_i) + \frac{\partial}{\partial r}(A\rho_i u_i) = AS_i$$

$$\frac{\partial}{\partial t}(A\rho_i u_i) + \frac{\partial}{\partial r}(A\rho_i u_i^2) + A\frac{\partial p_i}{\partial r} = A\rho_i\left(\frac{e}{m_i}E_{\parallel} - g\right) + A\frac{\delta M_i^{(z)}}{\delta t} + Au_i S_i$$

$$\begin{aligned} \frac{\partial}{\partial t}\left(\frac{1}{2}A\rho_i u_i^2 + \frac{1}{\gamma_i - 1}Ap_i\right) + \frac{\partial}{\partial r}\left(\frac{1}{2}A\rho_i u_i^3 + \frac{\gamma_i}{\gamma_i - 1}Au_i p_i\right) \\ = A\rho_i u_i\left(\frac{e}{m_i}E_{\parallel} - g\right) + \frac{\partial}{\partial r}(A\kappa_i \frac{\partial T_i}{\partial r}) + A\frac{\delta E_i}{\delta t} + Au_i \frac{\delta M_i}{\delta t} + \frac{1}{2}Au_i^2 S_i \end{aligned}$$

$$E_{\parallel} = -\frac{1}{en_e}\left[\frac{\partial}{\partial r}(p_e + \rho_e u_e^2) + \frac{A'}{A}\rho_e u_e^2\right] + \frac{1}{en_e}\frac{\partial}{\partial r}\left(\sum_i \frac{m_e}{m_i}[(u_e - u_i)S_i - \frac{\delta M_i}{\delta t}]\right) + \frac{\delta M_e}{\delta t}$$



Seven Ion Polar Wind Outflow Model : 7iPWOM

- New **Chemical** & **Collisional** Scheme
- **Suprathermal Electron: GLOW**
- Neutral Density: NRLMSISE-00

At each time step, solves for the n, T, v, and E_{||}

Developed from PWOM (Glocer et al., 2018), 7iPWOM solves Transport Equations and E_{||} equation for H⁺, He⁺, N⁺, O⁺, N₂⁺, NO⁺, O₂⁺

$$\frac{\partial}{\partial t}(A\rho_i) + \frac{\partial}{\partial r}(A\rho_i u_i) = AS_i \quad [1]$$

Source term

$$\frac{\partial}{\partial t}(A\rho_i u_i) + \frac{\partial}{\partial r}(A\rho_i u_i^2) + A \frac{\partial p_i}{\partial r} = A\rho_i \left(\frac{e}{m_i} E_{||} - g \right) + \frac{\partial}{\partial r}(A\kappa_i \frac{\partial T_i}{\partial r}) + A \frac{\partial S_i}{\partial t}$$

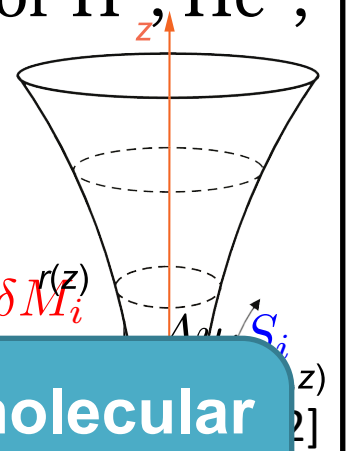
$$\frac{\partial}{\partial t} \left(\frac{1}{2} A\rho_i u_i^2 + \frac{1}{\gamma_i - 1} A p_i \right) + \frac{\partial}{\partial r} \left(\frac{1}{2} A\rho_i u_i^3 + \frac{1}{\gamma_i - 1} A p_i u_i \right) = A\rho_i u_i \left(\frac{e}{m_i} E_{||} - g \right) + \frac{\partial}{\partial r} (A\kappa_i \frac{\partial T_i}{\partial r}) + A \frac{\partial S_i}{\partial t}$$

$$E_{||} = -\frac{1}{en_e} \left[\frac{\partial}{\partial r} (p_e + \rho_e u_e^2) + \frac{A'}{A} \rho_e u_e^2 \right] + \frac{1}{en_e} \left(\sum_i \frac{m_e}{m_i} [(u_e - u_i) S_i - \frac{\delta M_i}{\delta t}] + \frac{\delta M_e}{\delta t} \right) \quad [3]$$

Blue: Chemistry Related; Red: Collision Related

Correct Equation

Static molecular ions (zero v and constant T)



Chemistry and Collisions

3iPWOM
 H^+ , He^+ , O^+

Chemistry process	Reaction rate($cm^3 s^{-1}$)	Reference
$O + h\nu \longrightarrow O^+ + e^-$	see text	
$O_2 + h\nu \longrightarrow O^+ + O + e^-$	see text	
$He + h\nu \longrightarrow He^+ + e^-$	see text	
$H + h\nu \longrightarrow H^+ + e^-$	see text	
$O + e^* \longrightarrow O^+ + 2e^-$	see text	
$O_2 + e^* \longrightarrow O^+ + O + 2e^-$	see text	
$He + e^* \longrightarrow He^+ + 2e^-$	see text	
$H + e^* \longrightarrow H^+ + 2e^-$	see text	
$O^+ + N_2 \longrightarrow N + NO^+$	1.2×10^{-12}	[R. Schunk & Nagy, 2009]
$O^+ + O_2 \longrightarrow O_2^+ + O$	2.1×10^{-11}	[R. Schunk & Nagy, 2009]
$He^+ + O_2 \longrightarrow O^+ + O + He$	9.7×10^{-10}	[R. Schunk & Nagy, 2009]
$He^+ + N_2 \longrightarrow N_2^+ + He$	5.2×10^{-10}	[R. Schunk & Nagy, 2009]
$He^+ + N_2 \longrightarrow N^+ + N + He$	7.8×10^{-10}	[R. Schunk & Nagy, 2009]
$H^+ + O \longrightarrow H + O^+$	$2.2 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]
$H + O^+ \longrightarrow H^+ + O$	$2.5 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]

Chemistry and Collisions

3iPWOM
H⁺, He⁺, O⁺

7iPWOM
H⁺, He⁺, N⁺, O⁺,
N₂⁺, NO⁺, O₂⁺

Chemistry process	Reaction rate($cm^3 s^{-1}$)	Reference
$O + h\nu \longrightarrow O^+ + e^-$	see text	
$O_2 + h\nu \longrightarrow O^+ + O + e^-$	see text	
$He + h\nu \longrightarrow He^+ + e^-$	see text	
$H + h\nu \longrightarrow H^+ + e^-$	see text	
$O + e^* \longrightarrow O^+ + 2e^-$	see text	
$O_2 + e^* \longrightarrow O^+ + O + 2e^-$	see text	
$He + e^* \longrightarrow He^+ + 2e^-$	see text	
$H + e^* \longrightarrow H^+ + 2e^-$	see text	
$O^+ + N_2 \longrightarrow N + NO^+$	1.2×10^{-12}	[R. Schunk & Nagy, 2009]
$O^+ + O_2 \longrightarrow O_2^+ + O$	2.1×10^{-11}	[R. Schunk & Nagy, 2009]
$He^+ + O_2 \longrightarrow O^+ + O + He$	9.7×10^{-10}	[R. Schunk & Nagy, 2009]
$He^+ + N_2 \longrightarrow N_2^+ + He$	5.2×10^{-10}	[R. Schunk & Nagy, 2009]
$He^+ + N_2 \longrightarrow N^+ + N + He$	7.8×10^{-10}	[R. Schunk & Nagy, 2009]
$H^+ + O \longrightarrow H + O^+$	$2.2 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]
$H + O^+ \longrightarrow H^+ + O$	$2.5 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]
$N + h\nu \longrightarrow N^+ + e^-$	see text	
$N_2 + h\nu \longrightarrow N^+ + N + e^-$	see text	
$N_2 + h\nu \longrightarrow N_2^+ + e^-$	see text	
$O_2 + h\nu \longrightarrow O_2^+ + e^-$	see text	
$NO + h\nu \longrightarrow N^+ + O + e^-$	see text	
$NO + h\nu \longrightarrow NO^+ + e^-$	see text	
$NO + h\nu \longrightarrow O^+ + N + e^-$	see text	
$N_2 + e^* \longrightarrow N_2^+ + 2e^-$	see text	
$O_2 + e^* \longrightarrow O_2^+ + 2e^-$	see text	
$N_2 + e^* \longrightarrow 2N^+ + 3e^-$	see text	
$N_2 + e^* \longrightarrow N^+ + N + 2e^-$	see text	
$N^+ + O_2 \longrightarrow NO^+ + O$	3.07×10^{-10}	[R. Schunk & Nagy, 2009]
$N^+ + O_2 \longrightarrow O_2^+ + N$	2.32×10^{-10}	[R. Schunk & Nagy, 2009]
$N^+ + O_2 \longrightarrow O^+ + NO$	4.6×10^{-11}	[R. Schunk & Nagy, 2009]
$N^+ + NO \longrightarrow NO^+ + N$	2×10^{-11}	[Lindinger et al., 1974]
$N^+ + O \longrightarrow N + O^+$	2.2×10^{-12}	[Richards & Voglozin, 2011]
$N^+ + H \longrightarrow N + H^+$	3.6×10^{-12}	[Harada et al., 2010]
$N_2^+ + N \longrightarrow N^+ + N_2$	10^{-11}	[Richards & Voglozin, 2011]
$N_2^+ + NO \longrightarrow NO^+ + N_2$	4.1×10^{-10}	[R. Schunk & Nagy, 2009]
$N_2^+ + O \longrightarrow NO^+ + N$	1.3×10^{-10}	[R. Schunk & Nagy, 2009]
$N_2^+ + O \longrightarrow O^+ + N_2$	1.0×10^{-11}	[R. Schunk & Nagy, 2009]
$N_2^+ + O_2 \longrightarrow O_2^+ + N_2$	5.0×10^{-11}	[R. Schunk & Nagy, 2009]
$O^+ + NO \longrightarrow NO^+ + O$	8.0×10^{-13}	[R. Schunk & Nagy, 2009]
$N^+ + e^- \longrightarrow N$	$3.6 \times 10^{-12} \times (\frac{250}{T_e})^{0.7}$	[R. Schunk & Nagy, 2009]
$N_2^+ + e^- \longrightarrow N + N$	$2.2 \times 10^{-7} \times (\frac{300}{T_e})^{0.39}$	[R. Schunk & Nagy, 2009]
$NO^+ + e^- \longrightarrow N + O$	$4.0 \times 10^{-7} \times (\frac{300}{T_e})^{0.5}$	[R. Schunk & Nagy, 2009]
$O_2^+ + e^- \longrightarrow O + O$	$2.4 \times 10^{-7} \times (\frac{300}{T_e})^{0.7}$	[R. Schunk & Nagy, 2009]

Chemistry and Collisions

New sources/losses for O⁺

3iPWOM
H⁺, He⁺, O⁺

7iPWOM
H⁺, He⁺, N⁺, O⁺,
N₂⁺, NO⁺, O₂⁺

Chemistry process	Reaction rate(cm ³ s ⁻¹)	Reference
O + hν → O ⁺ + e ⁻	see text	
O ₂ + hν → O ⁺ + O + e ⁻	see text	
He + hν → He ⁺ + e ⁻	see text	
H + hν → H ⁺ + e ⁻	see text	
O + e* → O ⁺ + 2e ⁻	see text	
O ₂ + e* → O ⁺ + O + 2e ⁻	see text	
He + e* → He ⁺ + 2e ⁻	see text	
H + e* → H ⁺ + 2e ⁻	see text	
O ⁺ + N ₂ → N + NO ⁺	1.2 × 10 ⁻¹²	[R. Schunk & Nagy, 2009]
O ⁺ + O ₂ → O ₂ ⁺ + O	2.1 × 10 ⁻¹¹	[R. Schunk & Nagy, 2009]
He ⁺ + O ₂ → O ⁺ + O + He	9.7 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
He ⁺ + N ₂ → N ₂ ⁺ + He	5.2 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
He ⁺ + N ₂ → N ⁺ + N + He	7.8 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
H ⁺ + O → H + O ⁺	2.2 × 10 ⁻¹¹ × T _e ^{0.5}	[R. Schunk & Nagy, 2009]
H + O ⁺ → H ⁺ + O	2.5 × 10 ⁻¹¹ × T _e ^{0.5}	[R. Schunk & Nagy, 2009]
N + hν → N ⁺ + e ⁻	see text	
N ₂ + hν → N ⁺ + N + e ⁻	see text	
N ₂ + hν → N ₂ ⁺ + e ⁻	see text	
O ₂ + hν → O ₂ ⁺ + e ⁻	see text	
NO + hν → N ⁺ + O + e ⁻	see text	
NO + hν → NO ⁺ + e ⁻	see text	
NO + hν → O ⁺ + N + e ⁻	see text	
N ₂ + e* → N ₂ ⁺ + 2e ⁻	see text	
O ₂ + e* → O ₂ ⁺ + 2e ⁻	see text	
N ₂ + e* → 2N ⁺ + 3e ⁻	see text	
N ₂ + e* → N ⁺ + N + 2e ⁻	see text	
N ⁺ + O ₂ → NO ⁺ + O	3.07 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
N ⁺ + O ₂ → O ₂ ⁺ + N	2.32 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
N ⁺ + O ₂ → O ⁺ + NO	4.6 × 10 ⁻¹¹	[R. Schunk & Nagy, 2009]
N ⁺ + NO → NO ⁺ + N	2 × 10 ⁻¹¹	[Lindinger et al., 1974]
N ⁺ + O → N + O ⁺	2.2 × 10 ⁻¹²	[Richards & Voglozin, 2011]
N ⁺ + H → N + H ⁺	3.6 × 10 ⁻¹²	[Harada et al., 2010]
N ₂ ⁺ + N → N ⁺ + N ₂	10 ⁻¹¹	[Richards & Voglozin, 2011]
N ₂ ⁺ + NO → NO ⁺ + N ₂	4.1 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
N ₂ ⁺ + O → NO ⁺ + N	1.3 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
N ₂ ⁺ + O → O ⁺ + N ₂	1.0 × 10 ⁻¹¹	[R. Schunk & Nagy, 2009]
N ₂ ⁺ + O ₂ → O ₂ ⁺ + N ₂	5.0 × 10 ⁻¹¹	[R. Schunk & Nagy, 2009]
O ⁺ + NO → NO ⁺ + O	8.0 × 10 ⁻¹³	[R. Schunk & Nagy, 2009]
N ⁺ + e → N	3.6 × 10 ⁻¹² × (250/T _e) ^{0.7}	[R. Schunk & Nagy, 2009]
N ₂ ⁺ + e ⁻ → N + N	2.2 × 10 ⁻⁷ × (300/T _e) ^{0.39}	[R. Schunk & Nagy, 2009]
NO ⁺ + e ⁻ → N + O	4.0 × 10 ⁻⁷ × (300/T _e) ^{0.5}	[R. Schunk & Nagy, 2009]
O ₂ ⁺ + e ⁻ → O + O	2.4 × 10 ⁻⁷ × (300/T _e) ^{0.7}	[R. Schunk & Nagy, 2009]

Chemistry and Collisions

New sources/losses for O⁺

New sources for H⁺

3iPWOM
H⁺, He⁺, O⁺

7iPWOM
H⁺, He⁺, N⁺, O⁺,
N₂⁺, NO⁺, O₂⁺

Chemistry process	Reaction rate(cm ³ s ⁻¹)	Reference
O + hν → O ⁺ + e ⁻	see text	
O ₂ + hν → O ⁺ + O + e ⁻	see text	
He + hν → He ⁺ + e ⁻	see text	
H + hν → H ⁺ + e ⁻	see text	
O + e* → O ⁺ + 2e ⁻	see text	
O ₂ + e* → O ⁺ + O + 2e ⁻	see text	
He + e* → He ⁺ + 2e ⁻	see text	
H + e* → H ⁺ + 2e ⁻	see text	
O ⁺ + N ₂ → N + NO ⁺	1.2 × 10 ⁻¹²	[R. Schunk & Nagy, 2009]
O ⁺ + O ₂ → O ₂ ⁺ + O	2.1 × 10 ⁻¹¹	[R. Schunk & Nagy, 2009]
He ⁺ + O ₂ → O ⁺ + O + He	9.7 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
He ⁺ + N ₂ → N ₂ ⁺ + He	5.2 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
He ⁺ + N ₂ → N ⁺ + N + He	7.8 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
H ⁺ + O → H + O ⁺	2.2 × 10 ⁻¹¹ × T _e ^{0.5}	[R. Schunk & Nagy, 2009]
H + O ⁺ → H ⁺ + O	2.5 × 10 ⁻¹¹ × T _e ^{0.5}	[R. Schunk & Nagy, 2009]
N + hν → N ⁺ + e ⁻	see text	
N ₂ + hν → N ⁺ + N + e ⁻	see text	
N ₂ + hν → N ₂ ⁺ + e ⁻	see text	
O ₂ + hν → O ₂ ⁺ + e ⁻	see text	
NO + hν → N ⁺ + O + e ⁻	see text	
NO + hν → NO ⁺ + e ⁻	see text	
NO + hν → O ⁺ + N + e ⁻	see text	
N ₂ + e* → N ₂ ⁺ + 2e ⁻	see text	
O ₂ + e* → O ₂ ⁺ + 2e ⁻	see text	
N ₂ + e* → 2N ⁺ + 3e ⁻	see text	
N ₂ + e* → N ⁺ + N + 2e ⁻	see text	
N ⁺ + O ₂ → NO ⁺ + O	3.07 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
N ⁺ + O ₂ → O ₂ ⁺ + N	2.32 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
N ⁺ + O ₂ → O ⁺ + NO	4.6 × 10 ⁻¹¹	[R. Schunk & Nagy, 2009]
N ⁺ + NO → NO ⁺ + N	2 × 10 ⁻¹¹	[Lindinger et al., 1974]
N ⁺ + O → N + O ⁺	2.2 × 10 ⁻¹²	[Richards & Voglozin, 2011]
N ⁺ + H → N + H ⁺	3.6 × 10 ⁻¹²	[Harada et al., 2010]
N ₂ ⁺ + N → N ⁺ + N ₂	10 ⁻¹¹	[Richards & Voglozin, 2011]
N ₂ ⁺ + NO → NO ⁺ + N ₂	4.1 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
N ₂ ⁺ + O → NO ⁺ + N	1.3 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
N ₂ ⁺ + O → O ⁺ + N ₂	1.0 × 10 ⁻¹¹	[R. Schunk & Nagy, 2009]
N ₂ ⁺ + O ₂ → O ₂ ⁺ + N ₂	5.0 × 10 ⁻¹¹	[R. Schunk & Nagy, 2009]
O ⁺ + NO → NO ⁺ + O	8.0 × 10 ⁻¹³	[R. Schunk & Nagy, 2009]
N ⁺ + e → N	3.6 × 10 ⁻¹² × (250/T _e) ^{0.7}	[R. Schunk & Nagy, 2009]
N ₂ ⁺ + e ⁻ → N + N	2.2 × 10 ⁻⁷ × (300/T _e) ^{0.39}	[R. Schunk & Nagy, 2009]
NO ⁺ + e ⁻ → N + O	4.0 × 10 ⁻⁷ × (300/T _e) ^{0.5}	[R. Schunk & Nagy, 2009]
O ₂ ⁺ + e ⁻ → O + O	2.4 × 10 ⁻⁷ × (300/T _e) ^{0.7}	[R. Schunk & Nagy, 2009]

Chemistry and Collisions

New sources/losses for O⁺

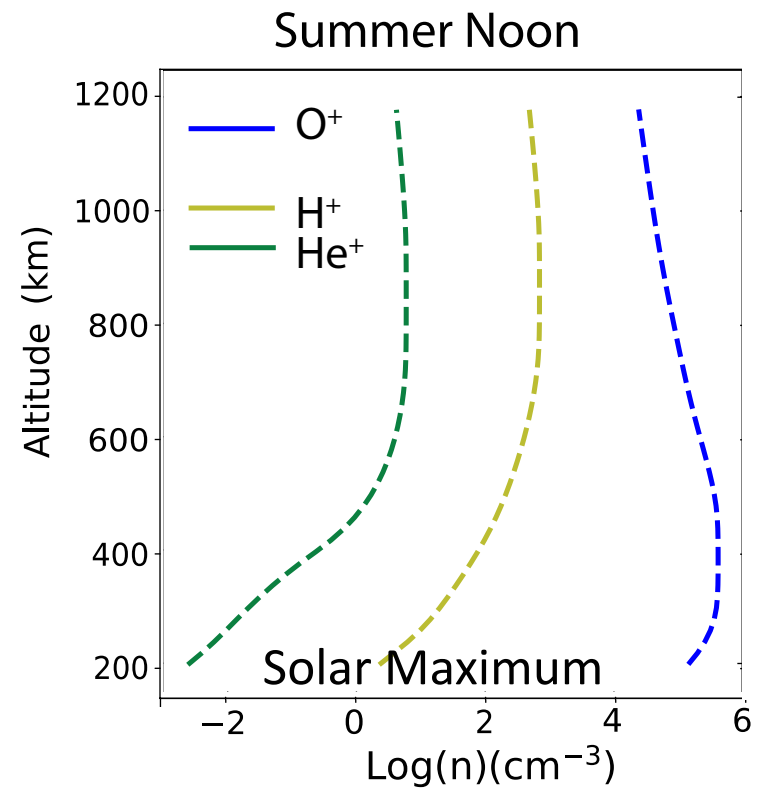
3iPWOM
H⁺, He⁺, O⁺

Suprathermal Electron (SE) Production

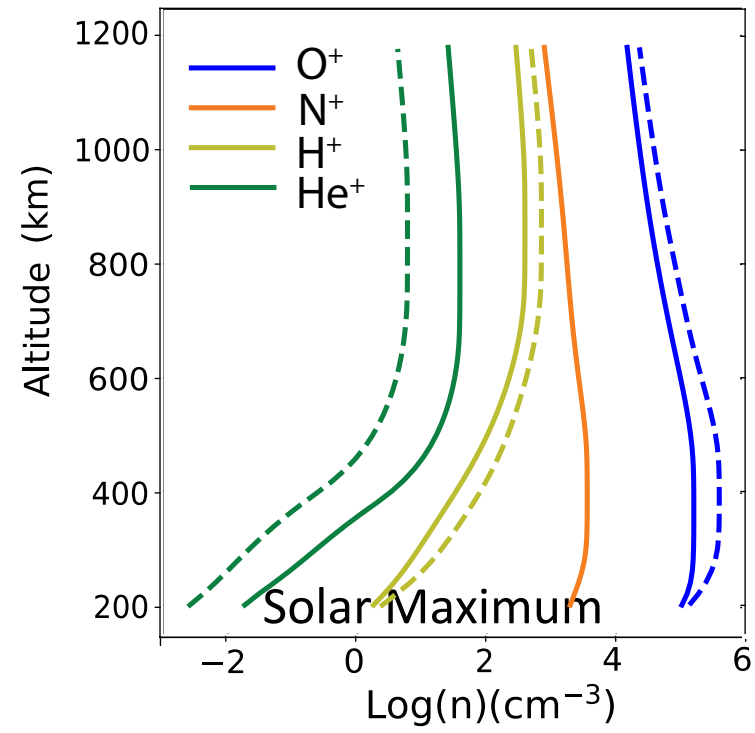
New sources for H⁺

7iPWOM
H⁺, He⁺, N⁺, O⁺,
N₂⁺, NO⁺, O₂⁺

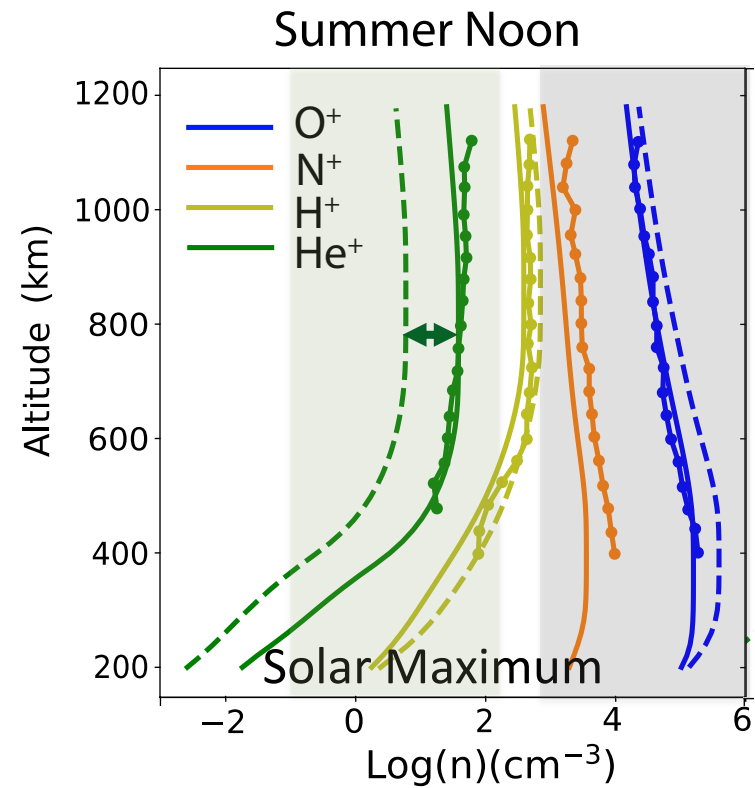
Chemistry process	Reaction rate(cm ³ s ⁻¹)	Reference
O + hν → O ⁺ + e ⁻	see text	
O ₂ + hν → O ⁺ + O + e ⁻	see text	
He + hν → He ⁺ + e ⁻	see text	
H + hν → H ⁺ + e ⁻	see text	
O + e* → O ⁺ + 2e ⁻	see text	
O ₂ + e* → O ⁺ + O + 2e ⁻	see text	
He + e* → He ⁺ + 2e ⁻	see text	
H + e* → H ⁺ + 2e ⁻	see text	
O ⁺ + N ₂ → N + NO ⁺	1.2 × 10 ⁻¹²	[R. Schunk & Nagy, 2009]
O ⁺ + O ₂ → O ₂ ⁺ + O	2.1 × 10 ⁻¹¹	[R. Schunk & Nagy, 2009]
He ⁺ + O ₂ → O ⁺ + O + He	9.7 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
He ⁺ + N ₂ → N ₂ ⁺ + He	5.2 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
He ⁺ + N ₂ → N ⁺ + N + He	7.8 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
H ⁺ + O → H + O ⁺	2.2 × 10 ⁻¹¹ × T _e ^{0.5}	[R. Schunk & Nagy, 2009]
H + O ⁺ → H ⁺ + O	2.5 × 10 ⁻¹¹ × T _e ^{0.5}	[R. Schunk & Nagy, 2009]
N + hν → N ⁺ + e ⁻	see text	
N ₂ + hν → N ⁺ + N + e ⁻	see text	
N ₂ + hν → N ₂ ⁺ + e ⁻	see text	
O ₂ + hν → O ₂ ⁺ + e ⁻	see text	
NO + hν → N ⁺ + O + e ⁻	see text	
NO + hν → NO ⁺ + e ⁻	see text	
NO + hν → O ⁺ + N + e ⁻	see text	
N ₂ + e* → N ₂ ⁺ + 2e ⁻	see text	
O ₂ + e* → O ₂ ⁺ + 2e ⁻	see text	
N ₂ + e* → 2N ⁺ + 3e ⁻	see text	
N ₂ + e* → N ⁺ + N + 2e ⁻	see text	
N ⁺ + O ₂ → NO ⁺ + O	3.07 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
N ⁺ + O ₂ → O ₂ ⁺ + N	2.32 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
N ⁺ + O ₂ → O ⁺ + NO	4.6 × 10 ⁻¹¹	[R. Schunk & Nagy, 2009]
N ⁺ + NO → NO ⁺ + N	2 × 10 ⁻¹¹	[Lindinger et al., 1974]
N ⁺ + O → N + O ⁺	2.2 × 10 ⁻¹²	[Richards & Voglozin, 2011]
N ⁺ + H → N + H ⁺	3.6 × 10 ⁻¹²	[Harada et al., 2010]
N ₂ ⁺ + N → N ⁺ + N ₂	10 ⁻¹¹	[Richards & Voglozin, 2011]
N ₂ ⁺ + NO → NO ⁺ + N ₂	4.1 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
N ₂ ⁺ + O → NO ⁺ + N	1.3 × 10 ⁻¹⁰	[R. Schunk & Nagy, 2009]
N ₂ ⁺ + O → O ⁺ + N ₂	1.0 × 10 ⁻¹¹	[R. Schunk & Nagy, 2009]
N ₂ ⁺ + O ₂ → O ₂ ⁺ + N ₂	5.0 × 10 ⁻¹¹	[R. Schunk & Nagy, 2009]
O ⁺ + NO → NO ⁺ + O	8.0 × 10 ⁻¹³	[R. Schunk & Nagy, 2009]
N ⁺ + e → N	3.6 × 10 ⁻¹² × (250/T _e) ^{0.7}	[R. Schunk & Nagy, 2009]
N ₂ ⁺ + e ⁻ → N + N	2.2 × 10 ⁻⁷ × (300/T _e) ^{0.39}	[R. Schunk & Nagy, 2009]
NO ⁺ + e ⁻ → N + O	4.0 × 10 ⁻⁷ × (300/T _e) ^{0.5}	[R. Schunk & Nagy, 2009]
O ₂ ⁺ + e ⁻ → O + O	2.4 × 10 ⁻⁷ × (300/T _e) ^{0.7}	[R. Schunk & Nagy, 2009]



Summer Noon



———— 7iPWOM
----- 3iPWOM



OGO-6 Data

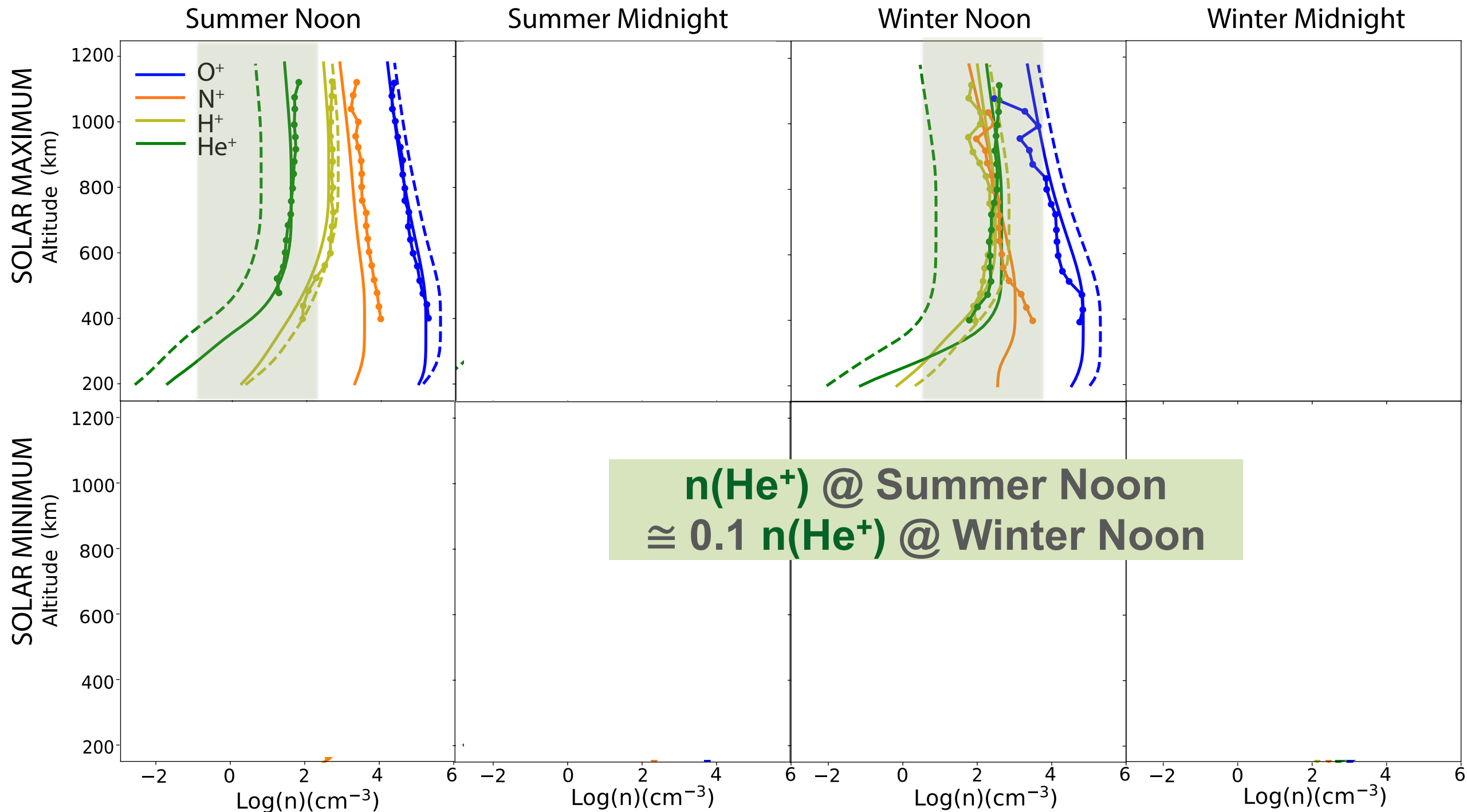
 7iPWOM

 3iPWOM

- Comparison with observations shows that the presence of **N⁺** improves the outflow solution for *all species*.

- He⁺** solution shows the biggest improvement, as 7iPWOM predicts a density **one order of magnitude higher than 3iPWOM**, aligned with observations.

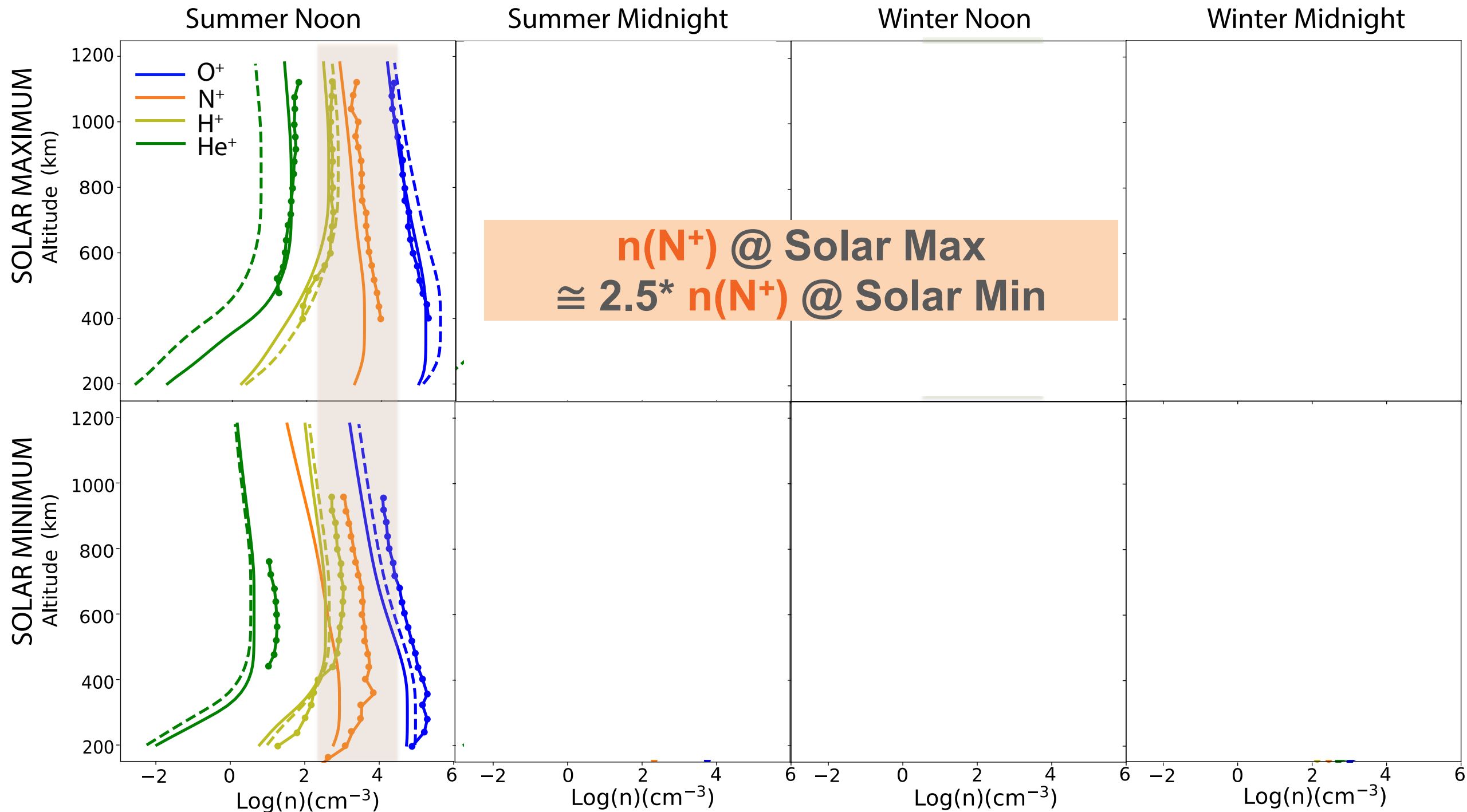
$$n(\text{N}^+) \cong 10\% \text{ of } n(\text{O}^+)$$



--- 3iPWOM

— 7iPWOM

●● DATA
(OGO6 or AE-C)

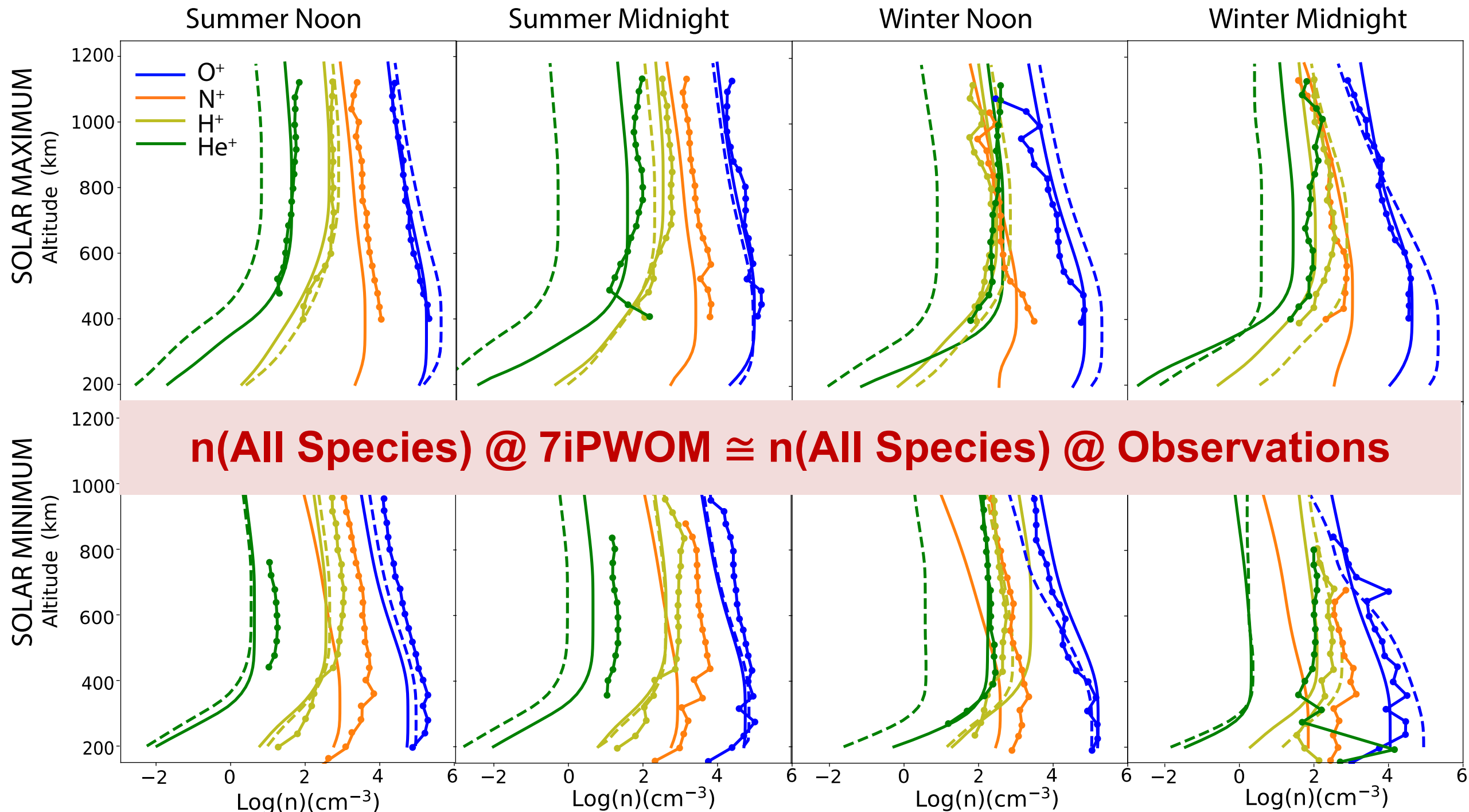


$n(N^+) @ \text{Solar Max}$
 $\cong 2.5 * n(N^+) @ \text{Solar Min}$

--- 3iPWOM

— 7iPWOM

●● DATA
 (OGO6 or AE-C)

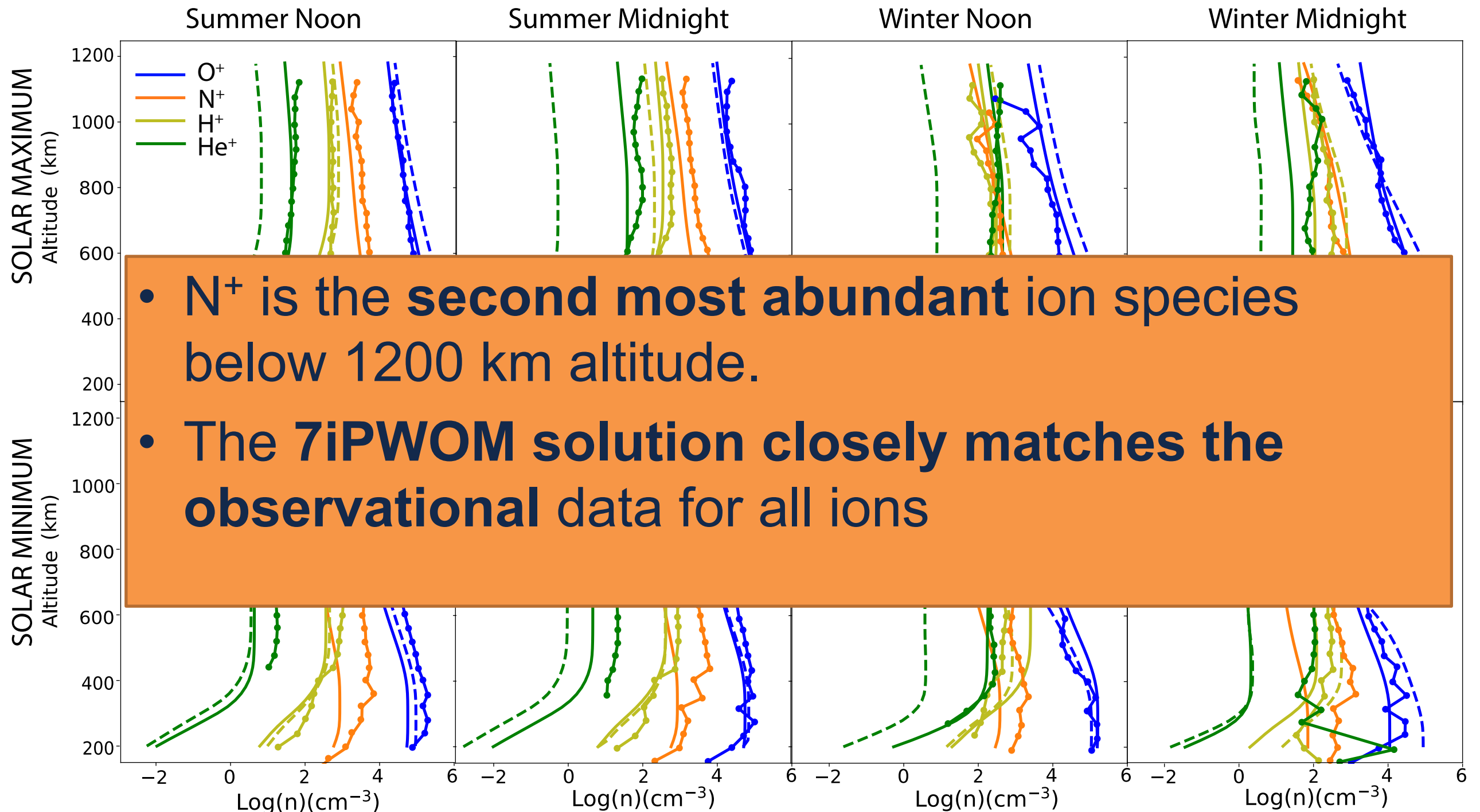


$n(\text{All Species}) @ 7iPWOM \cong n(\text{All Species}) @ \text{Observations}$

--- 3iPWOM

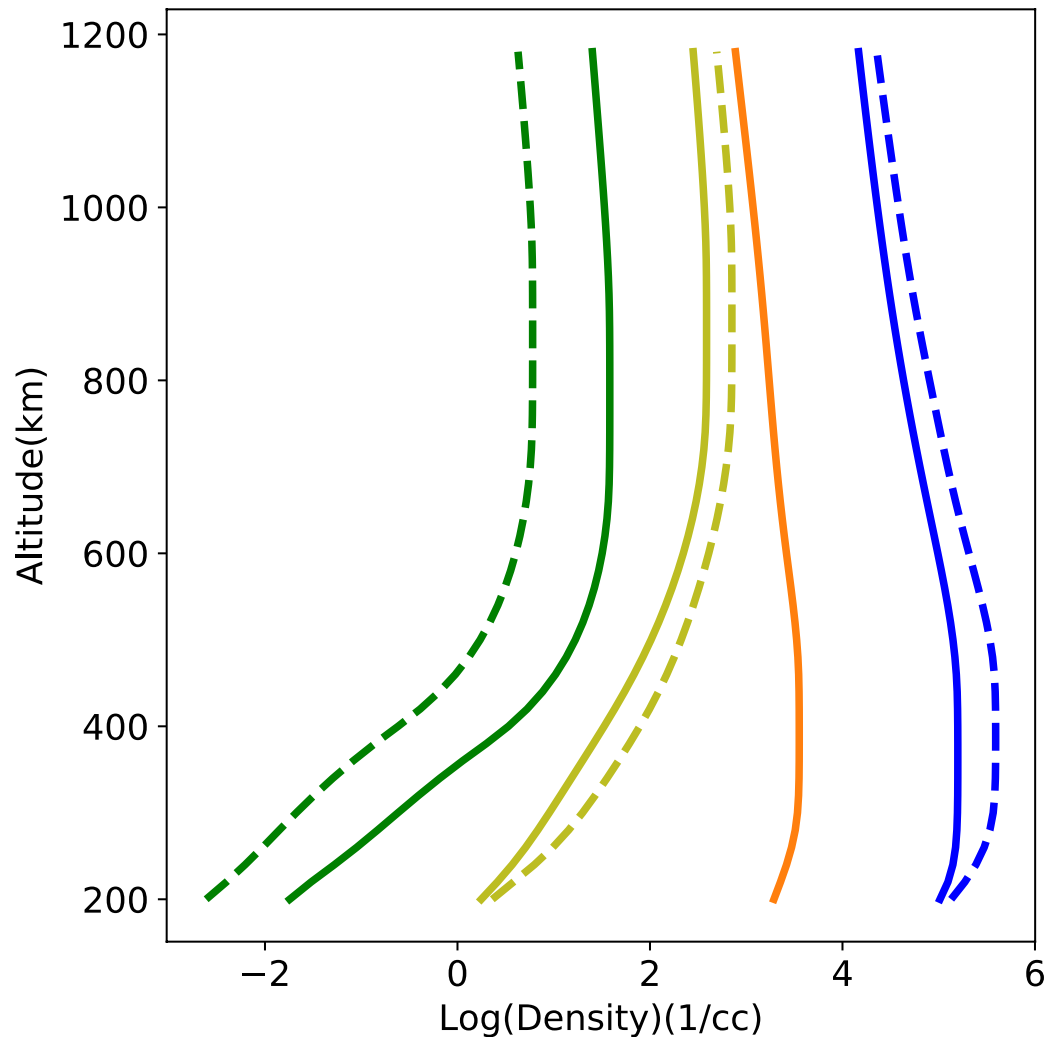
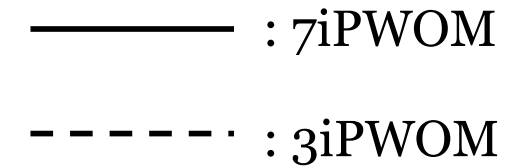
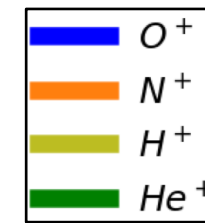
— 7iPWOM

●● DATA
(OGO6 or AE-C)



- N⁺ is the **second most abundant** ion species below 1200 km altitude.
- The **7iPWOM solution** closely matches the **observational data** for all ions

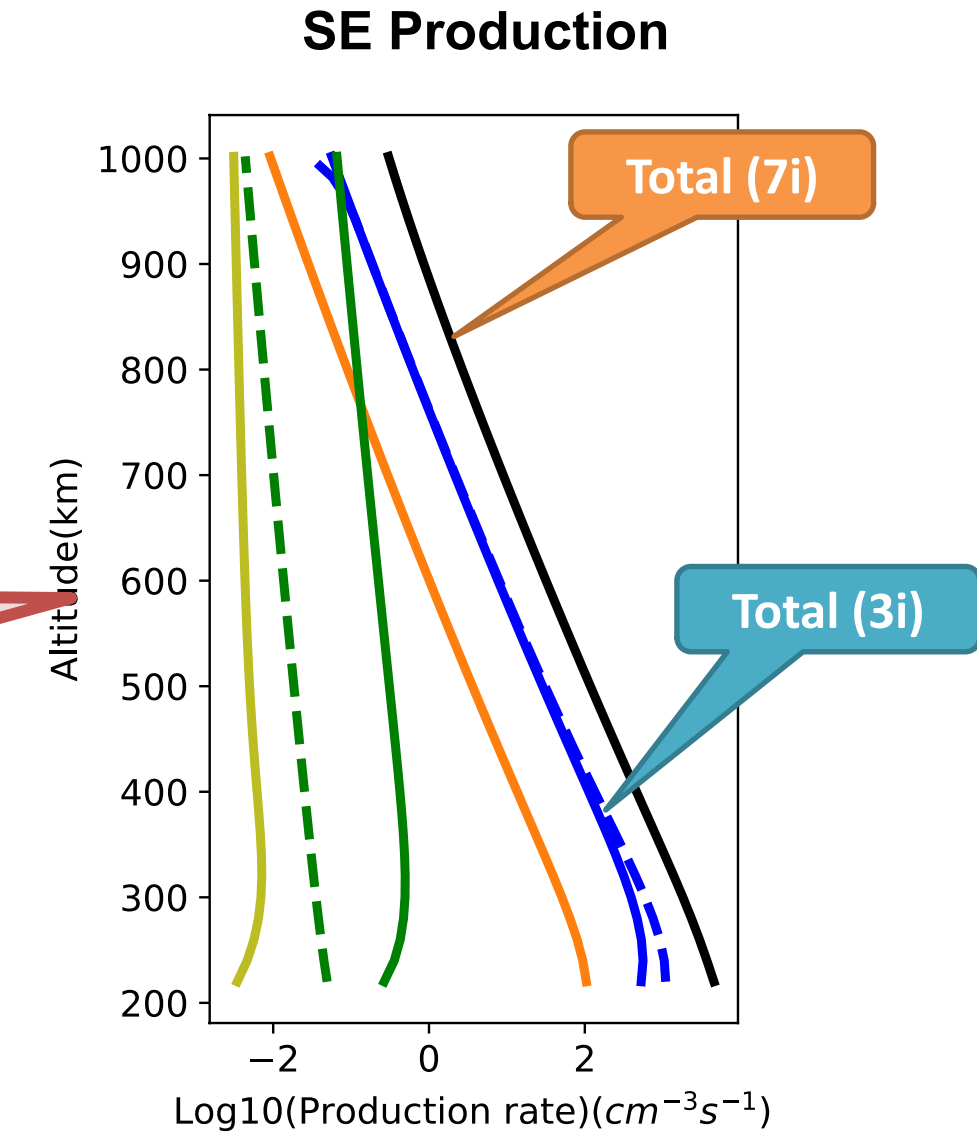
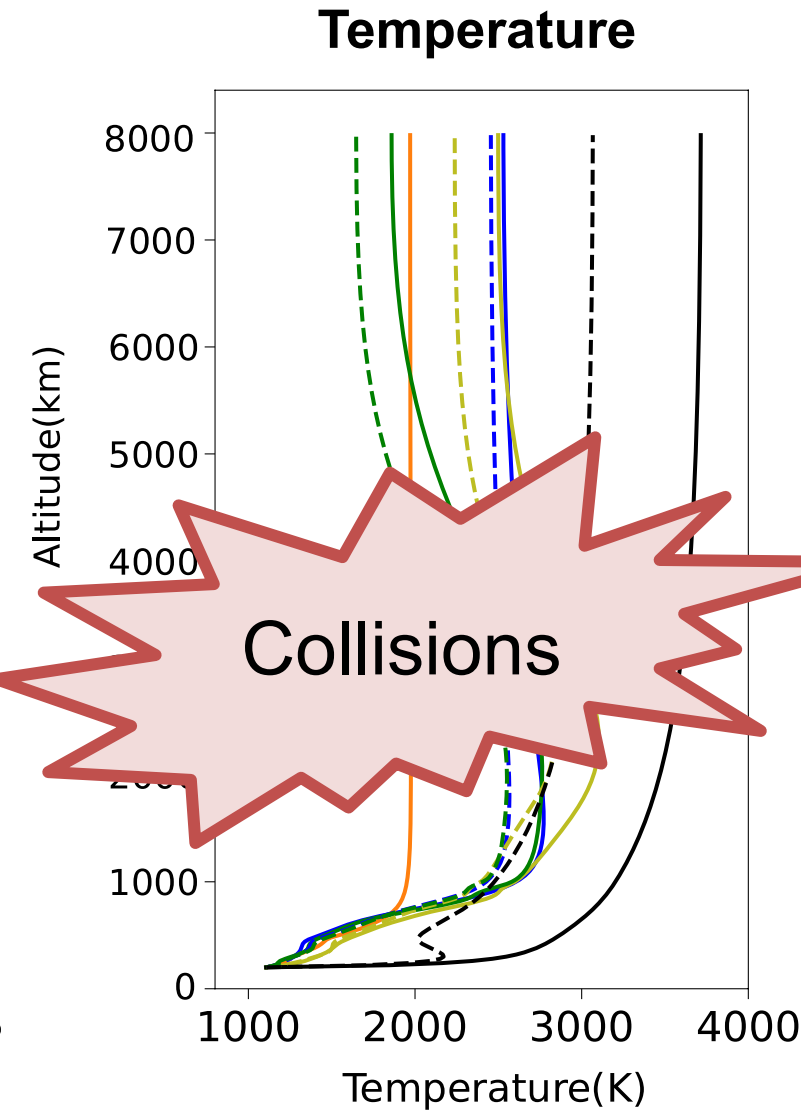
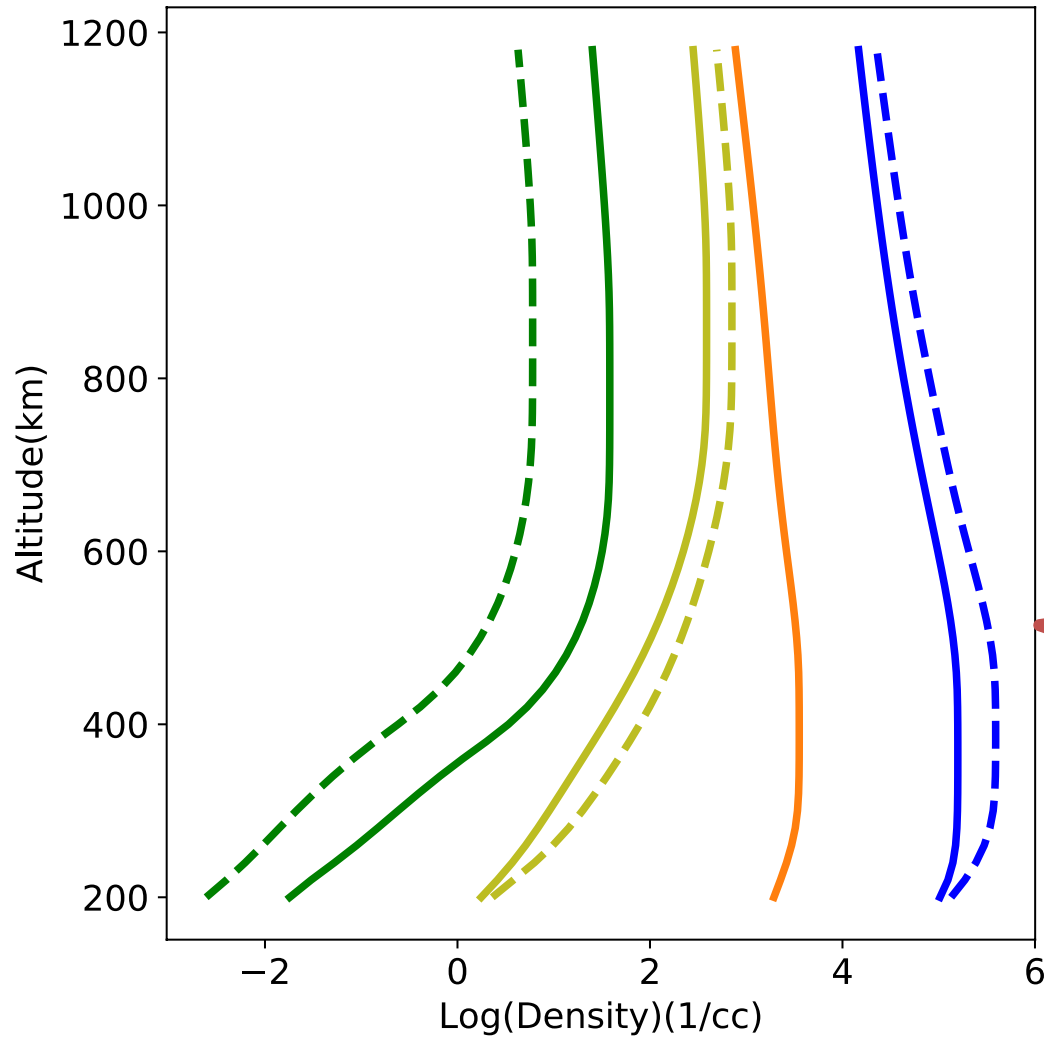
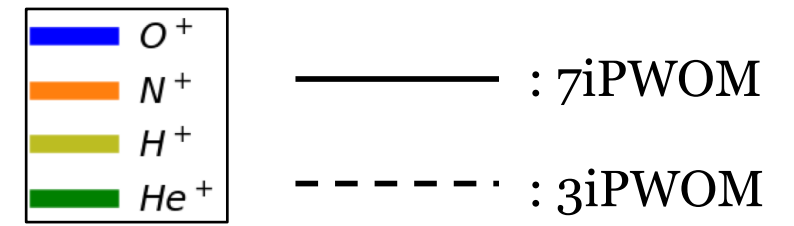
What causes these differences?



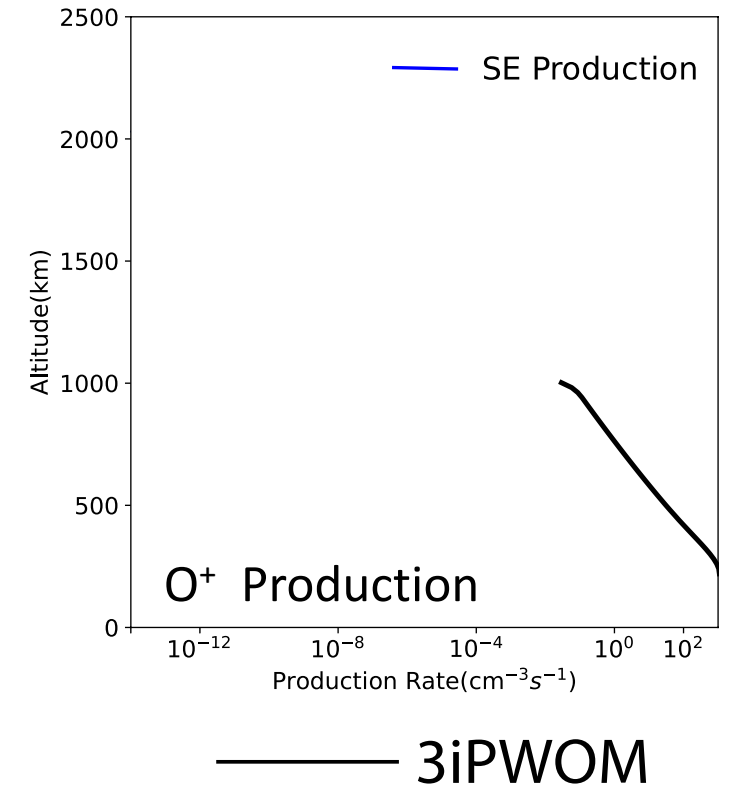
Presence of N^+ and molecular species leads to :

- A significant increase (~ 1 an order of magnitude) in He^+ density.
- H^+ solution improves as compared with measurements
- O^+ density profile better matches the data, and the density is a factor 2 larger.
- N^+ profile matches observations
- ***All species show an increase in temperature/energy.***

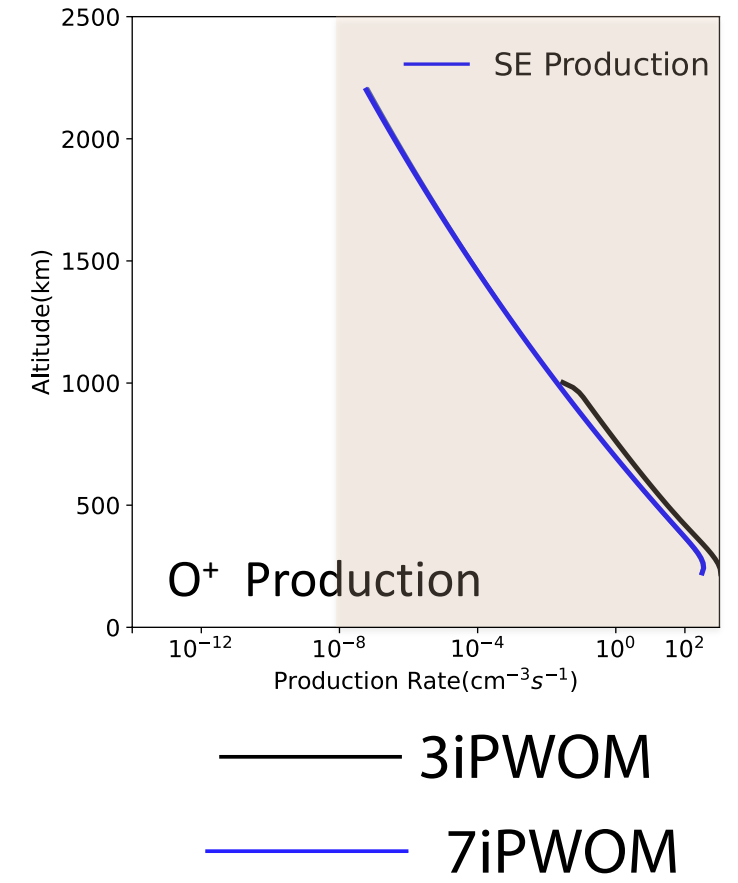
What causes these differences?



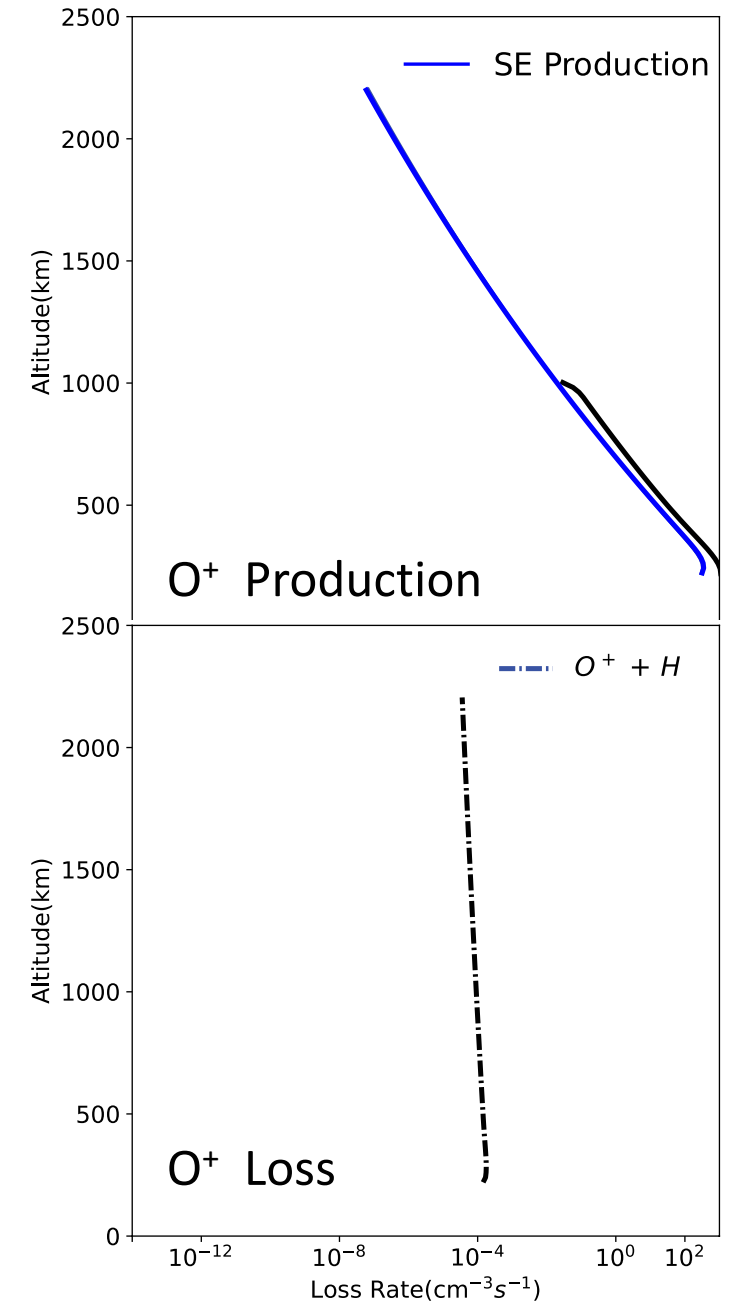
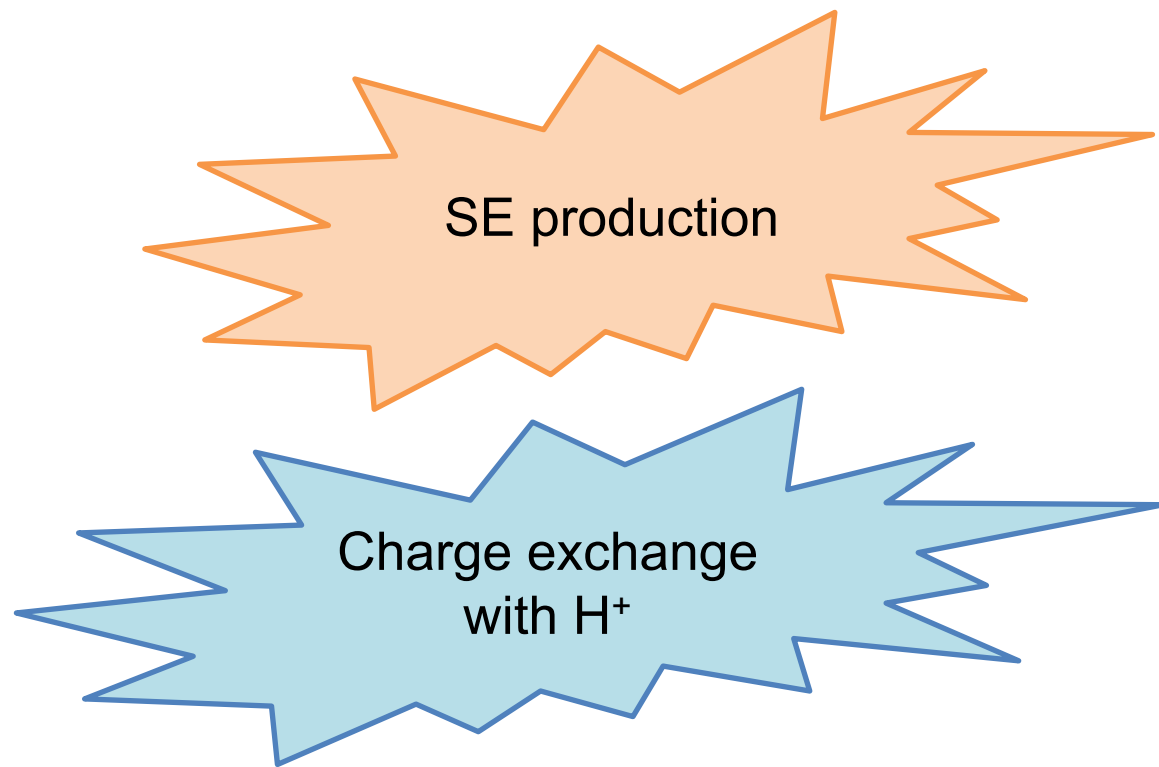
Chemistry?



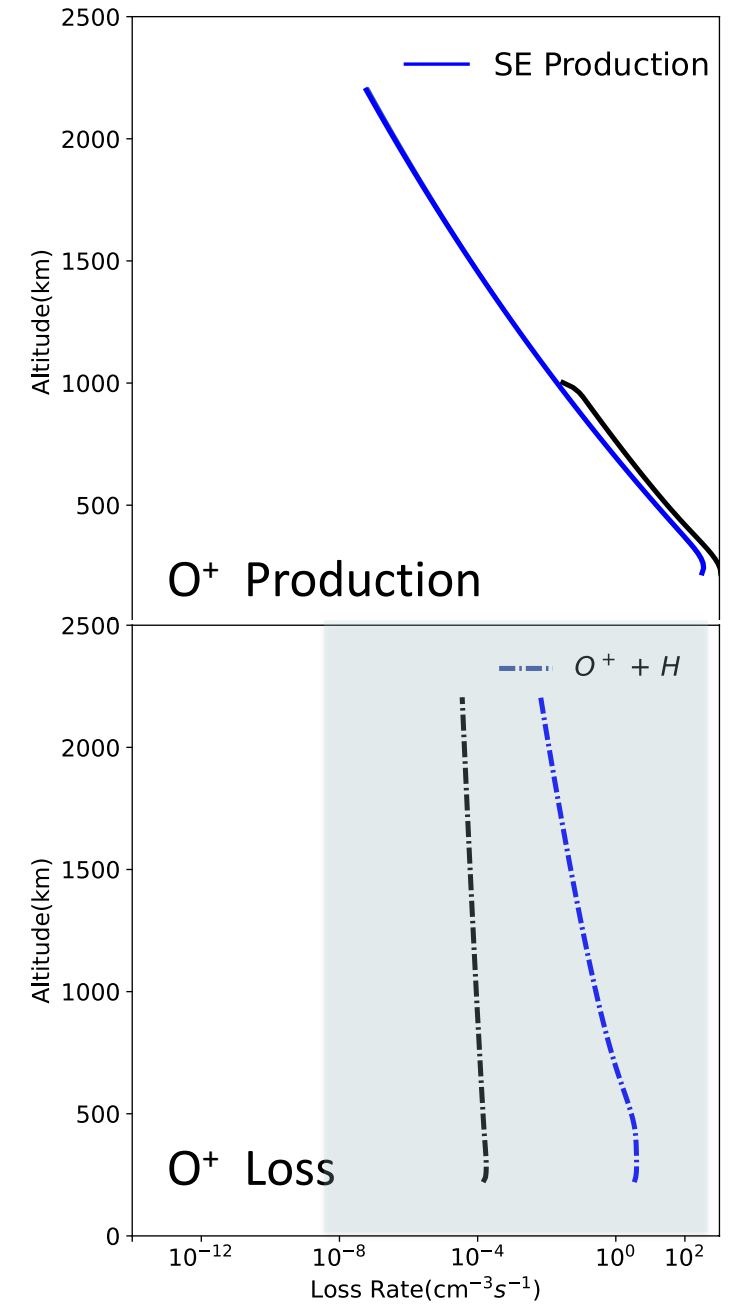
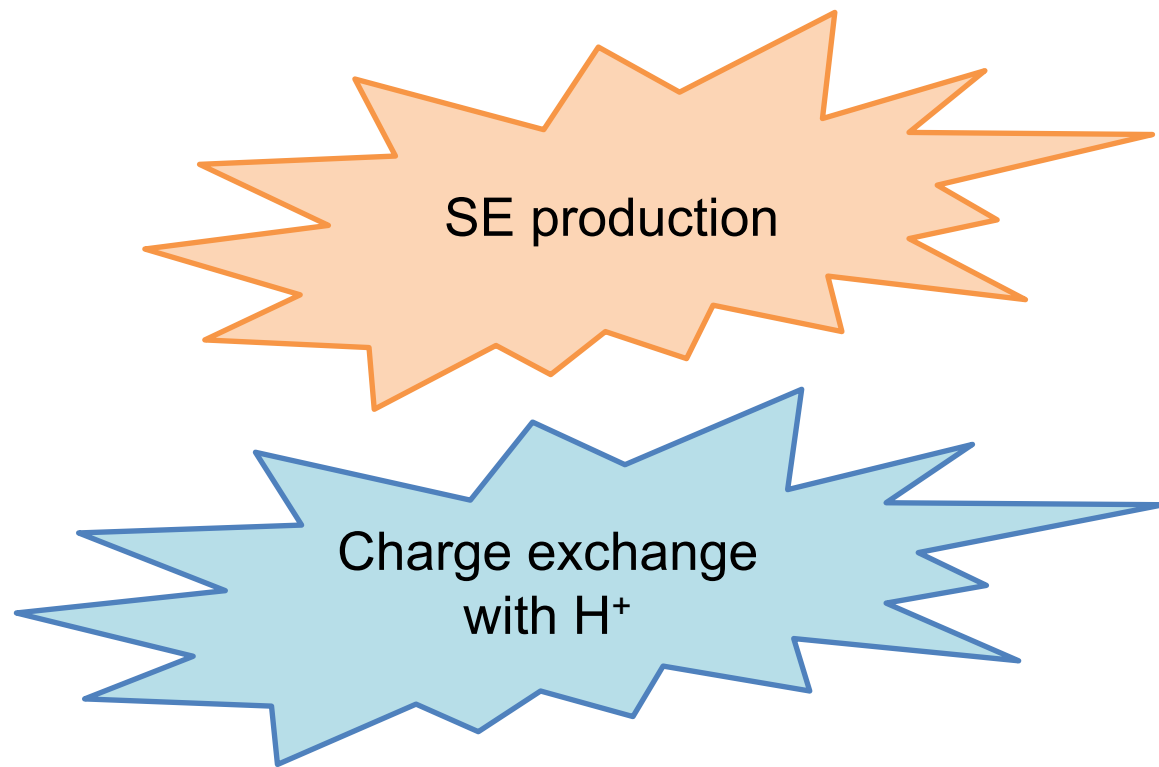
Chemistry?



Chemistry?



Chemistry?



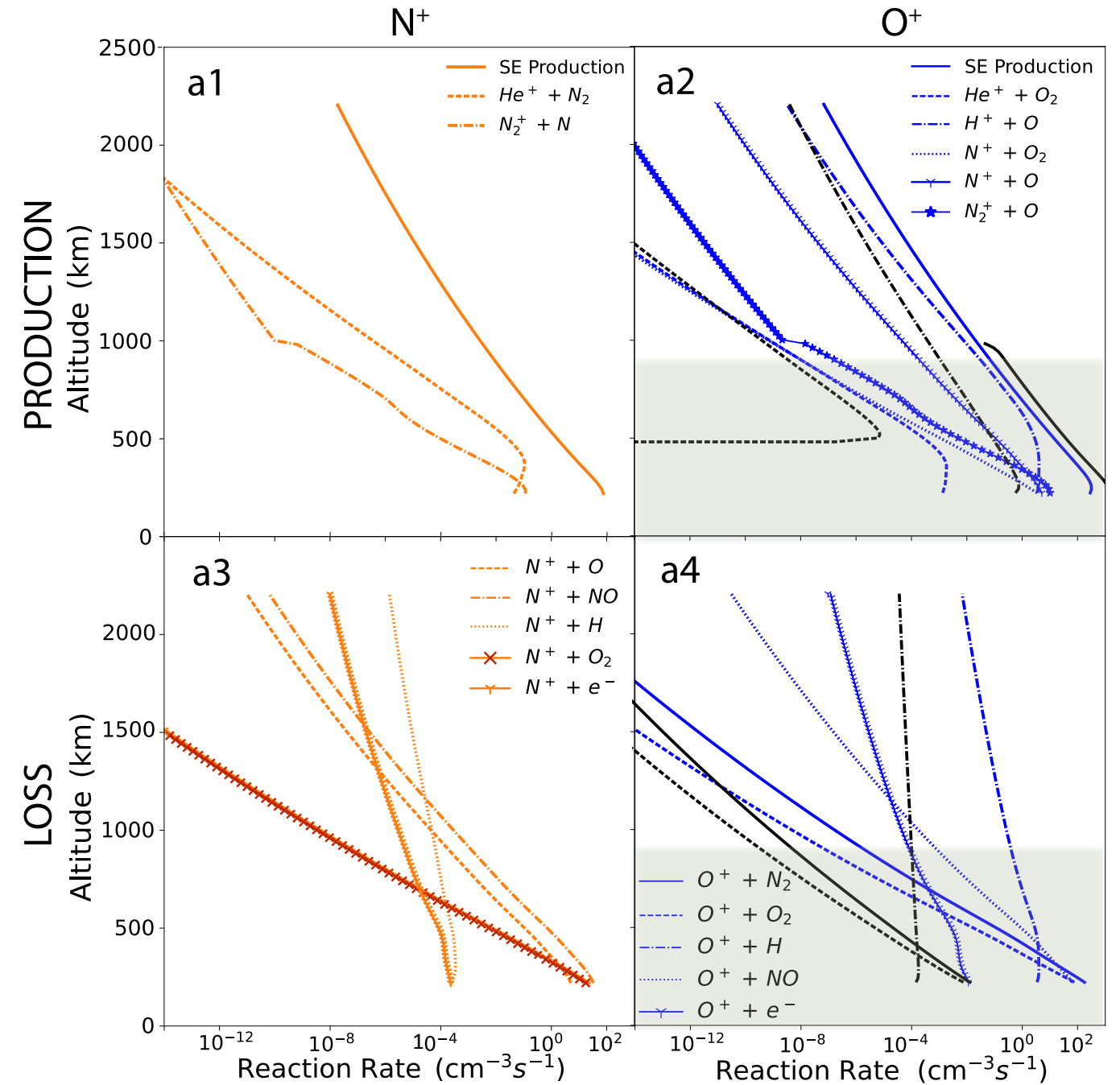
Chemistry?

Different Chemistry at low altitude

SE production

Charge exchange with H^+

(a) Production and Loss



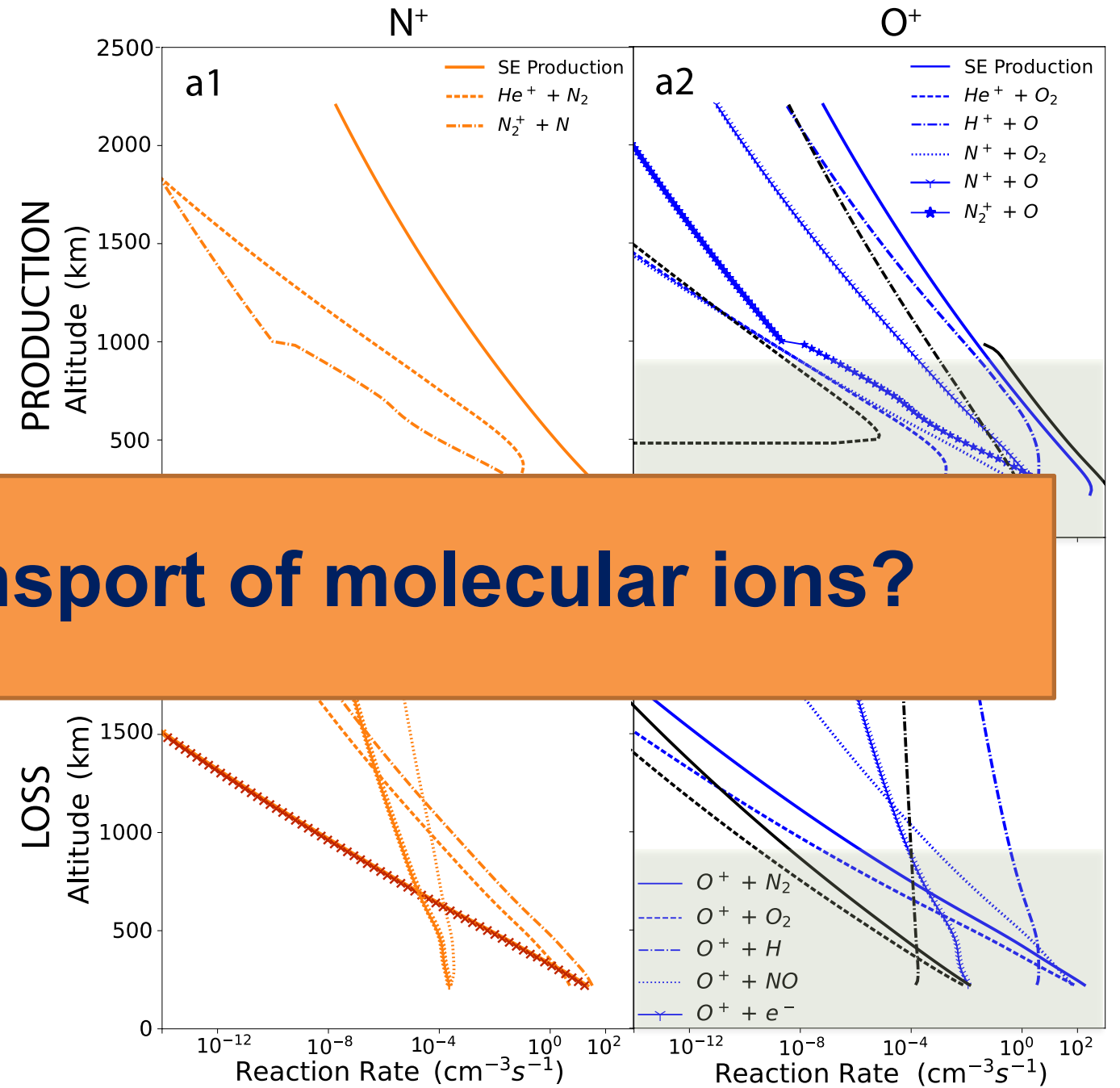
Chemistry?

Different Chemistry at low altitude

How about the transport of molecular ions?

Charge exchange with H^+

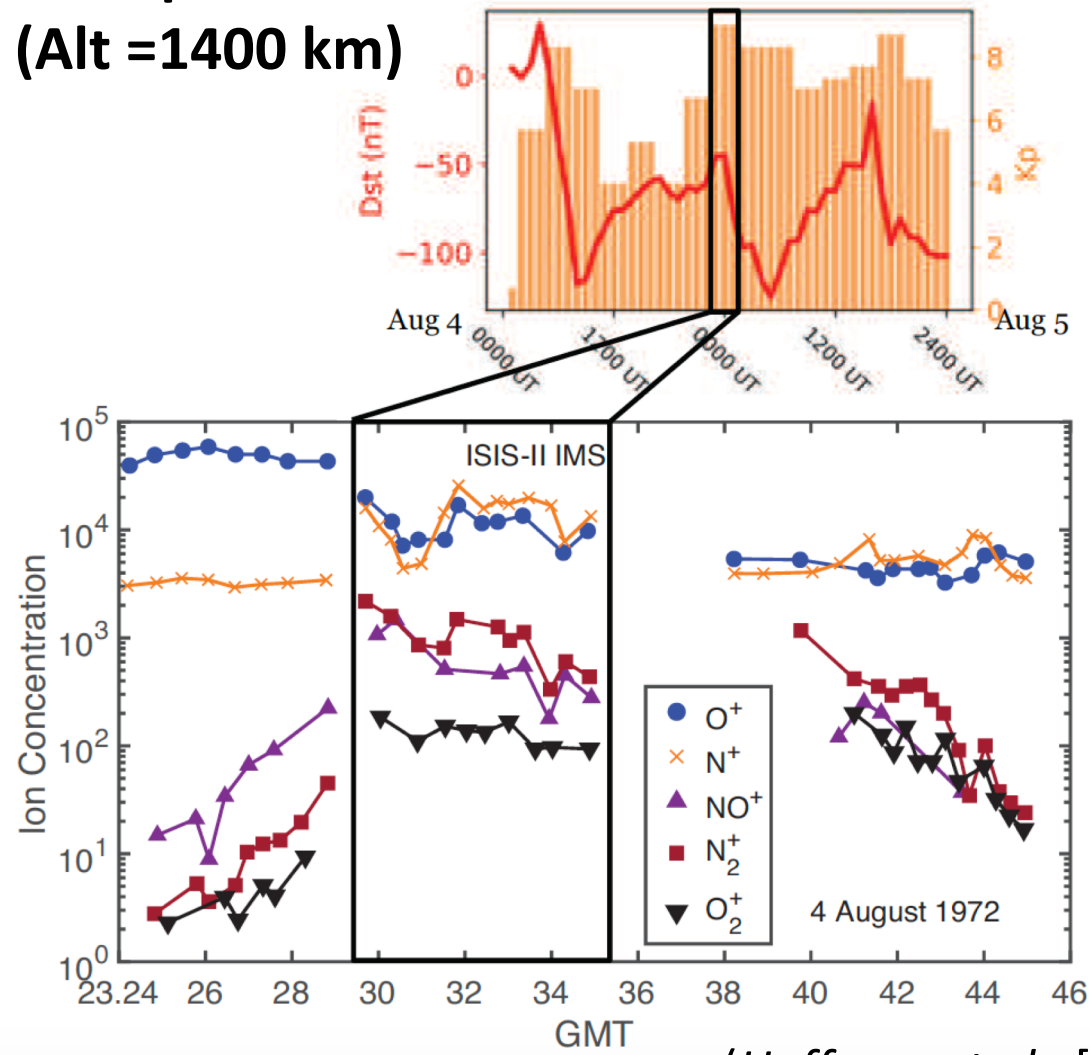
(a) Production and Loss



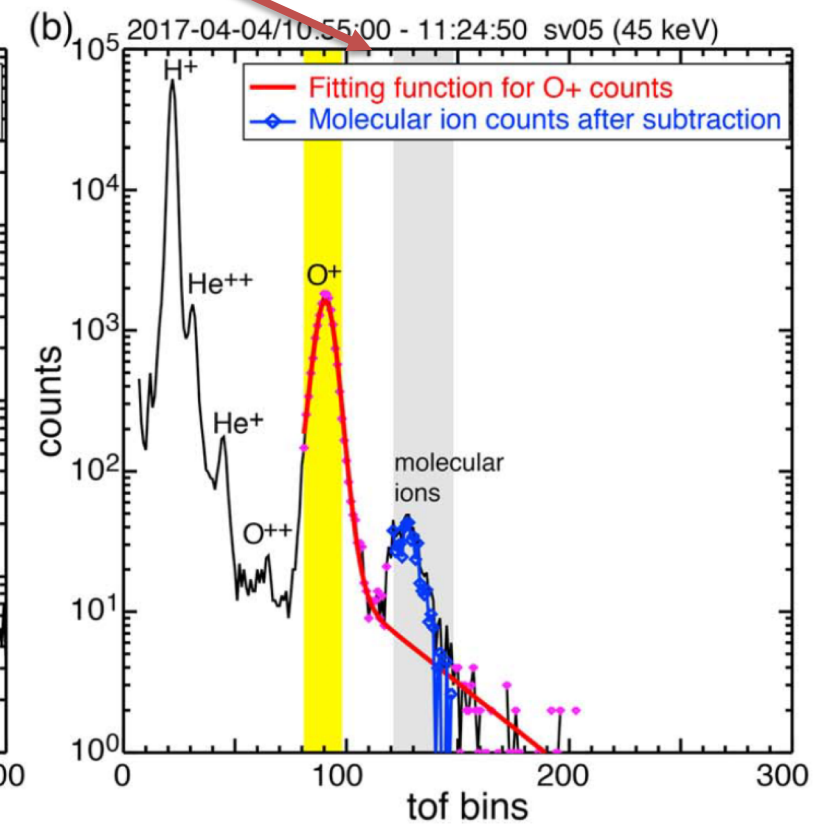
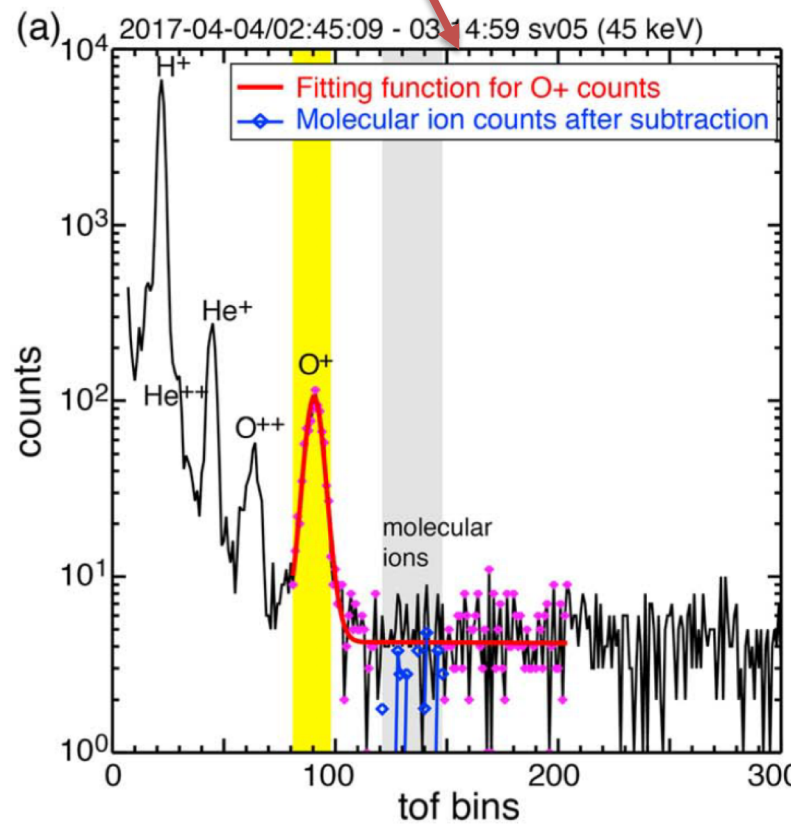
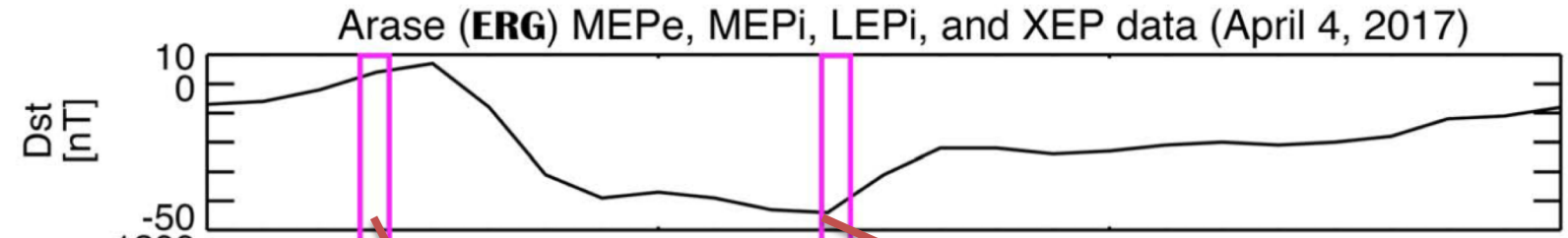
Observations of Molecular Ions

Inner Magnetosphere

Ionosphere
(Alt = 1400 km)



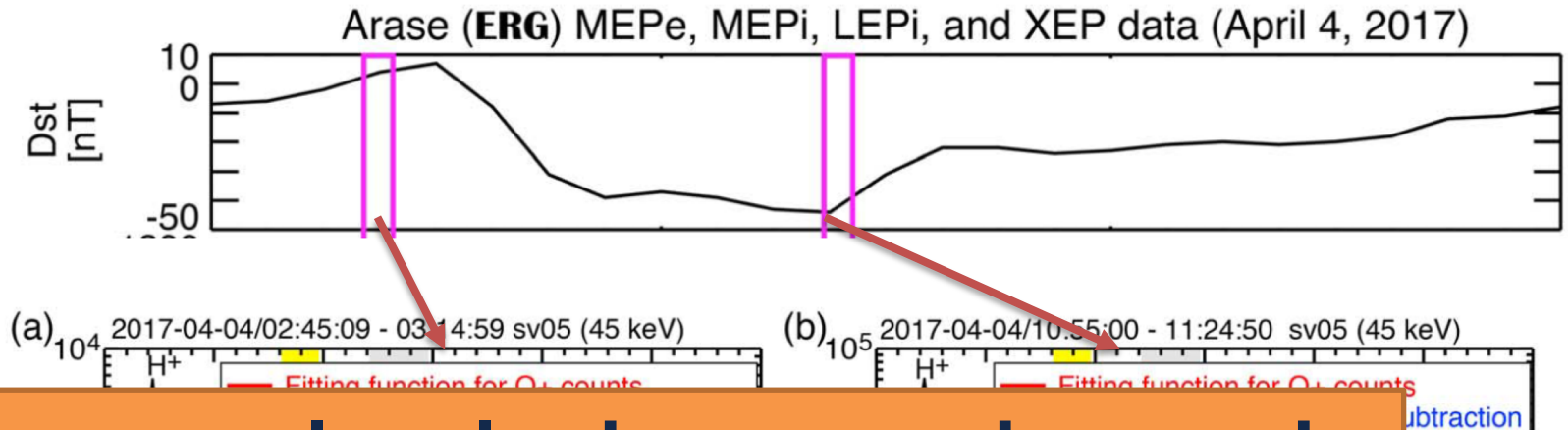
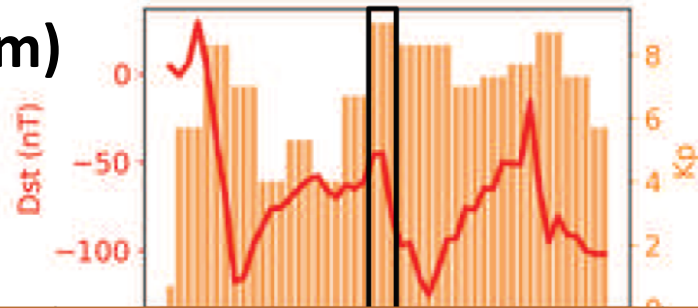
(Hoffman et al., [1974], JGR)



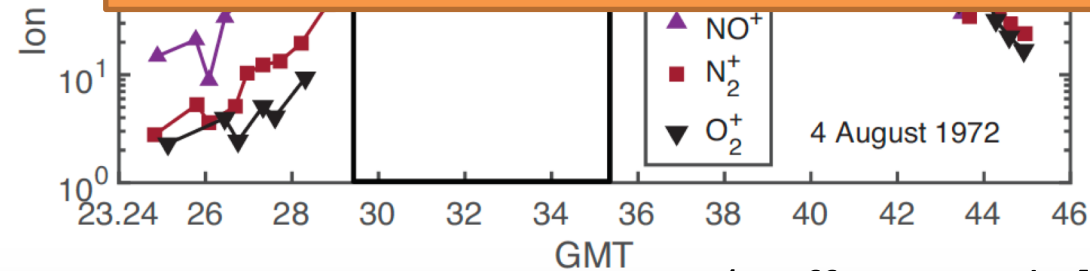
(Seki et al., [2019], GRL)

Observations of Molecular Ions

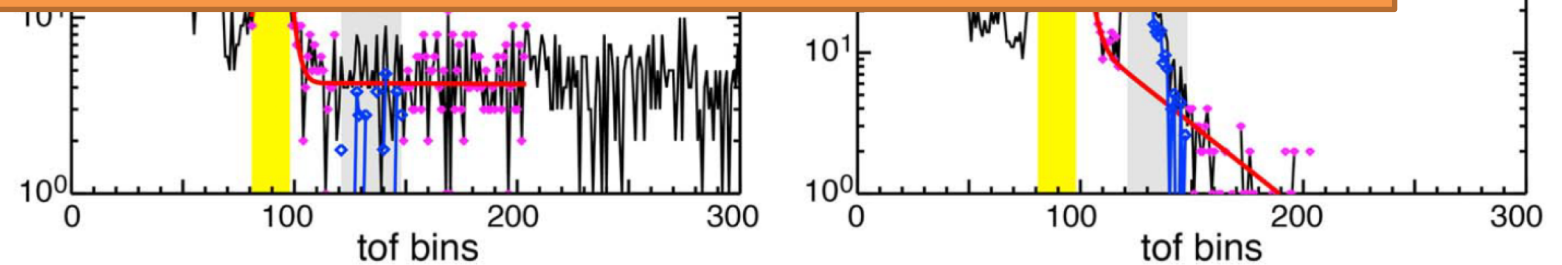
Ionosphere
(Alt = 1400 km)



- Even during moderate storms, **molecular ions are observed** both in the ionosphere and the magnetosphere.
- However, they are required to obtain sufficient energy in a very short time (possibly via **wave particle interactions**).



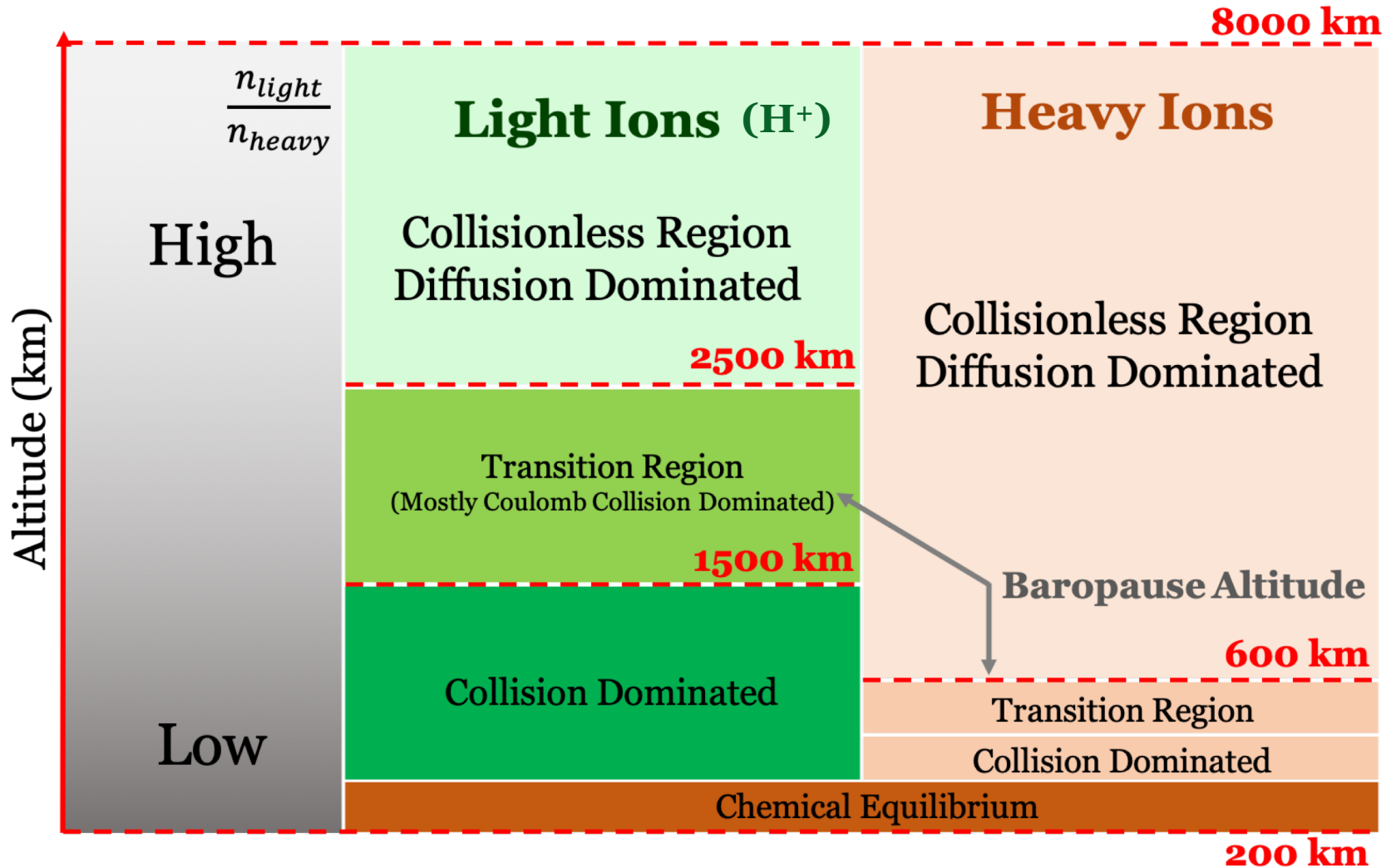
(Hoffman et al., [1974], JGR)



(Seki et al., [2019], GRL)

Our approach: 7iPWOM

(O⁺, N⁺, NO⁺)



ions

Hydro-dynamic

e⁻

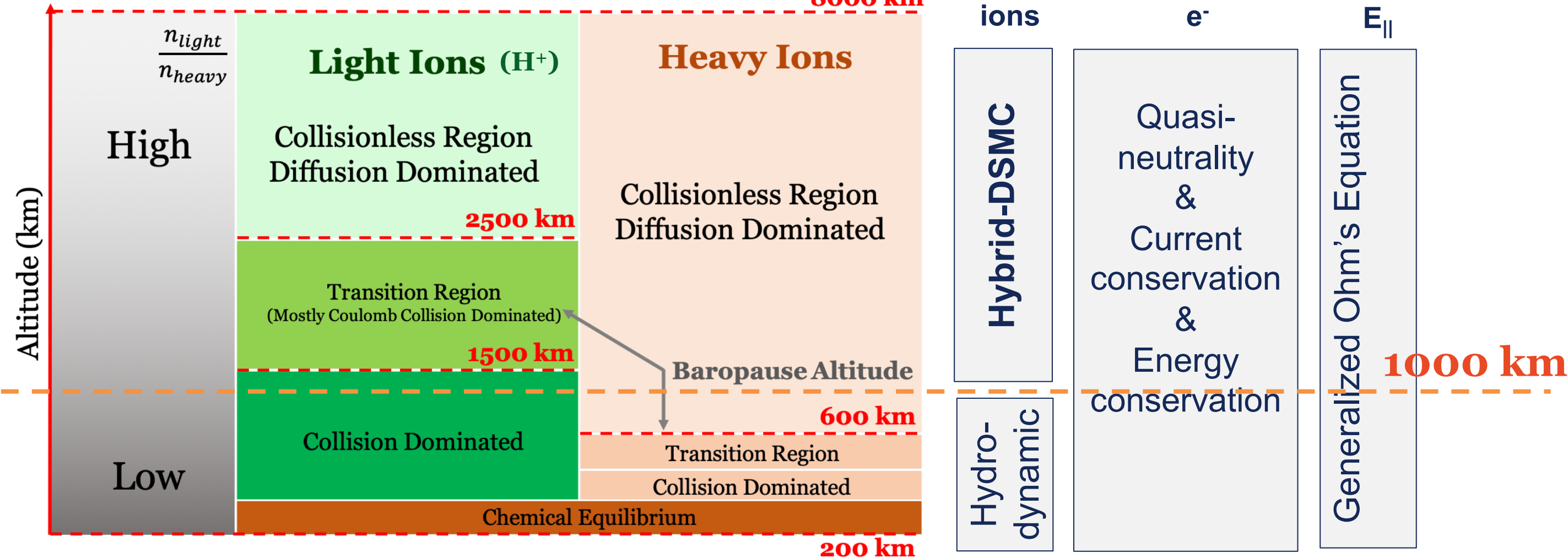
Quasi-neutrality & Current conservation & Energy conservation

E_{||}

Generalized Ohm's Equation

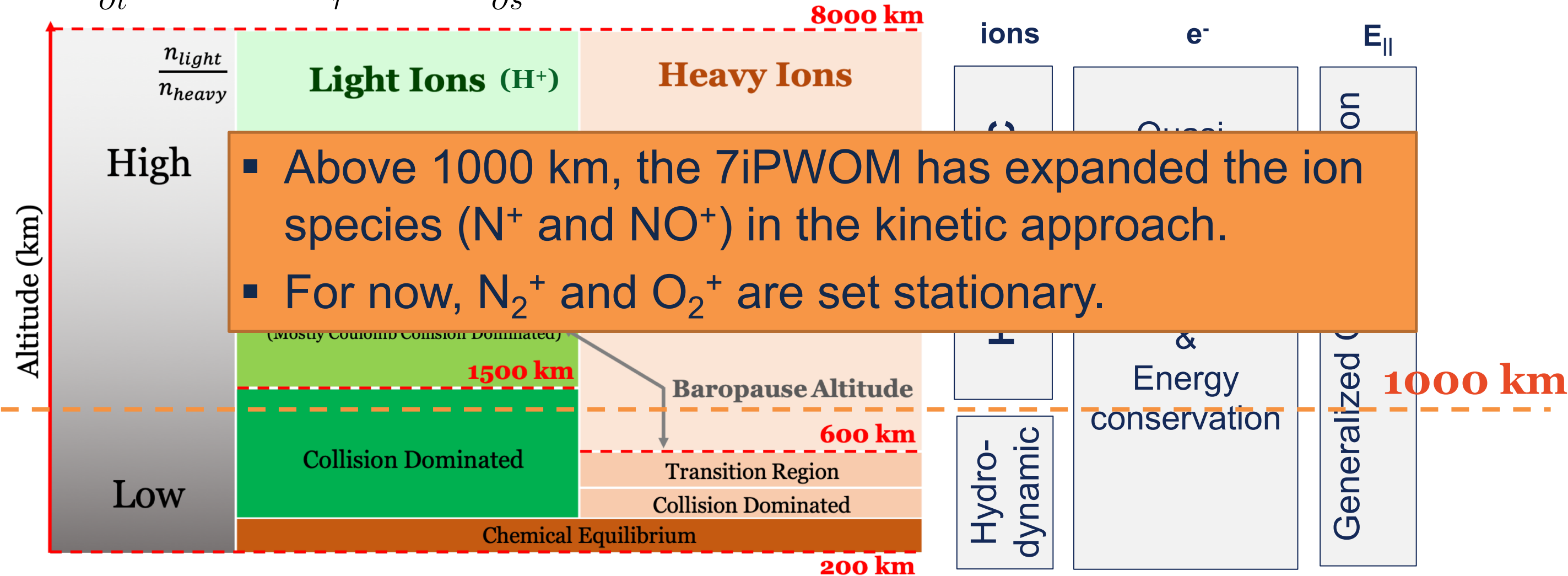
Our approach: 7iPWOM

$$m \frac{\partial v_{\parallel}}{\partial t} - qE_{\parallel} + \frac{GmM_{planet}}{r^2} + \mu \frac{\partial B}{\partial s} = 0 \quad (\text{O}^+, \text{N}^+, \text{NO}^+)$$

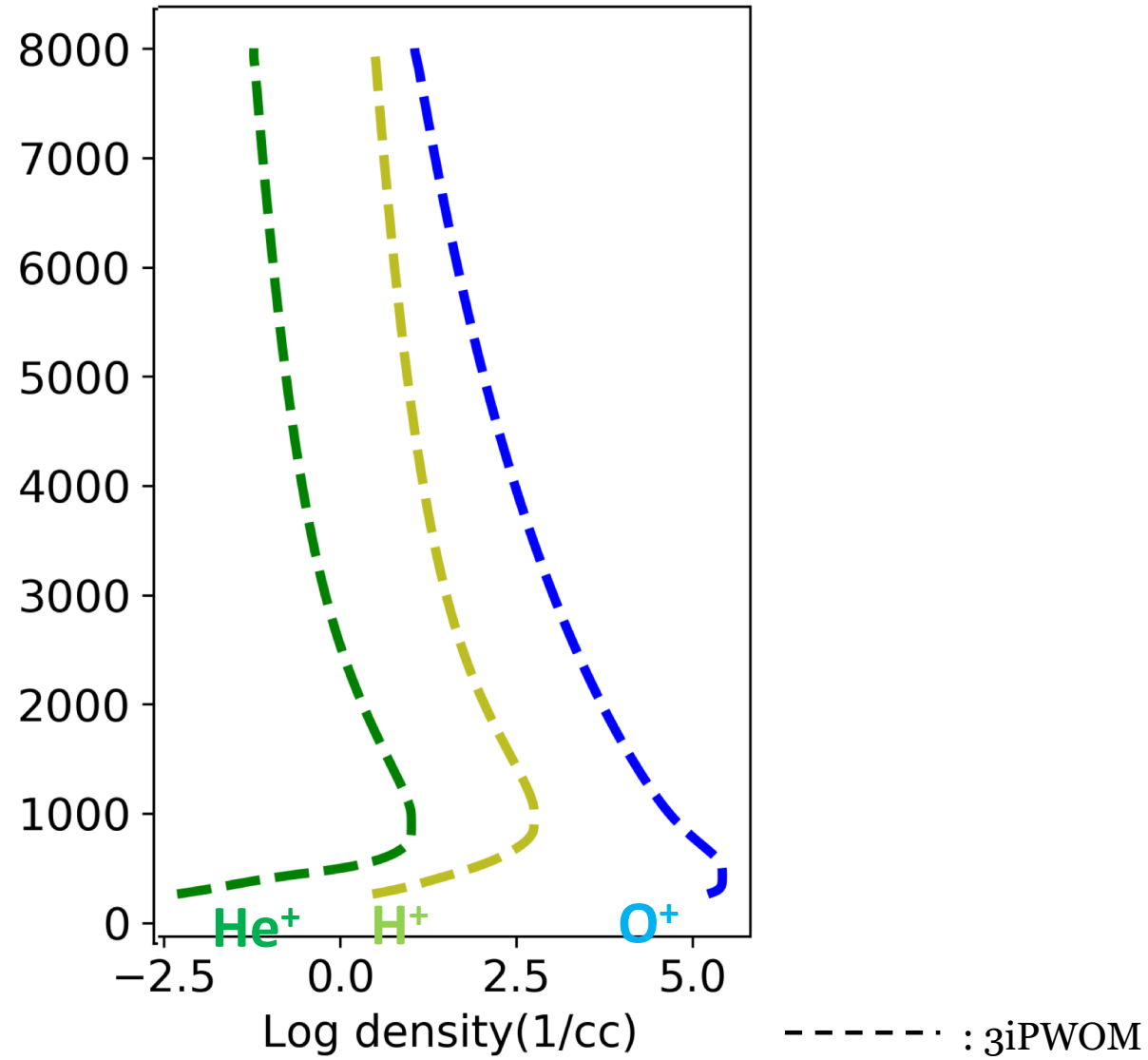


Our approach: 7iPWOM

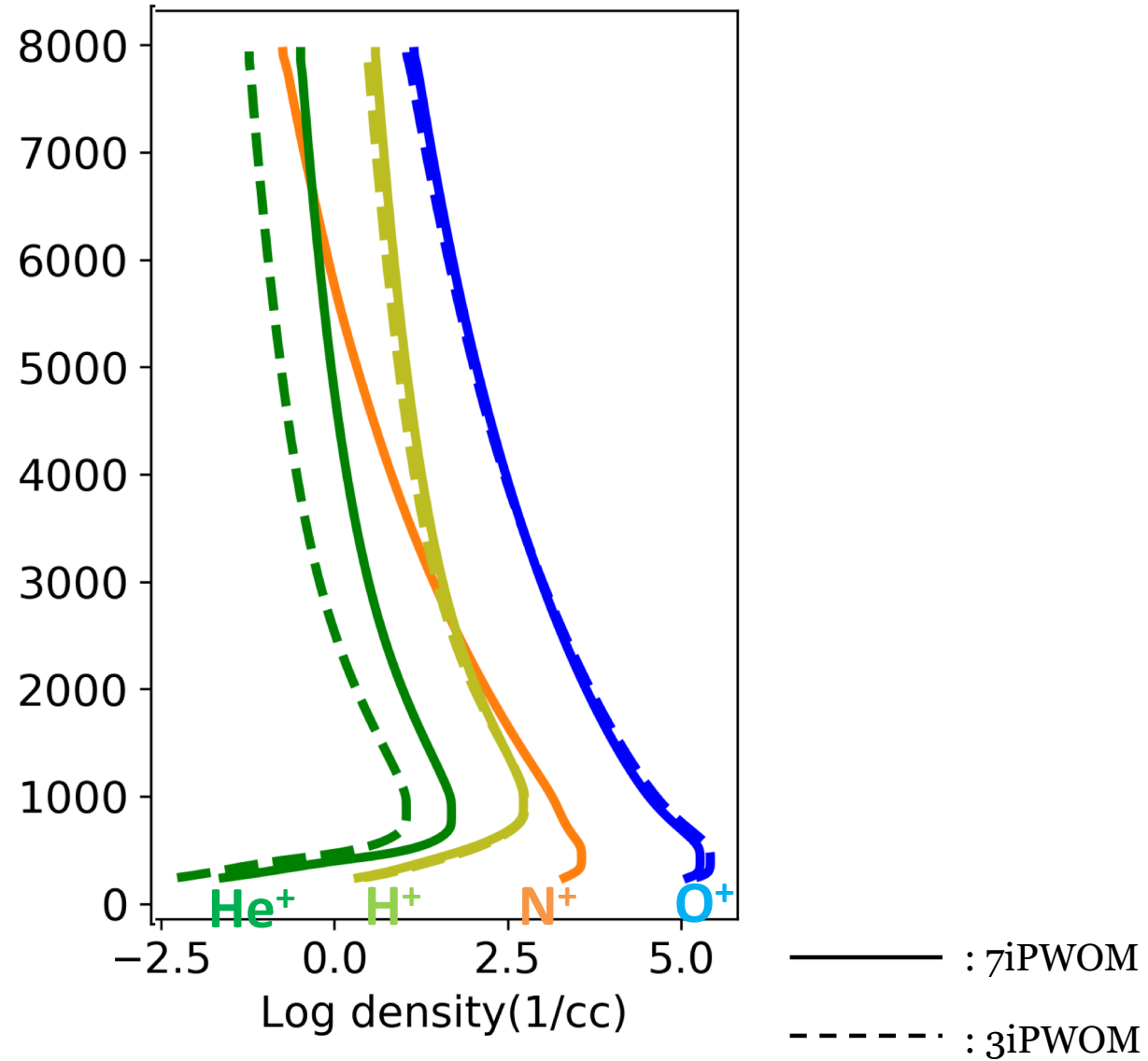
$$m \frac{\partial v_{\parallel}}{\partial t} - qE_{\parallel} + \frac{GmM_{planet}}{r^2} + \mu \frac{\partial B}{\partial s} = 0 \quad (\text{O}^+, \text{N}^+, \text{NO}^+)$$



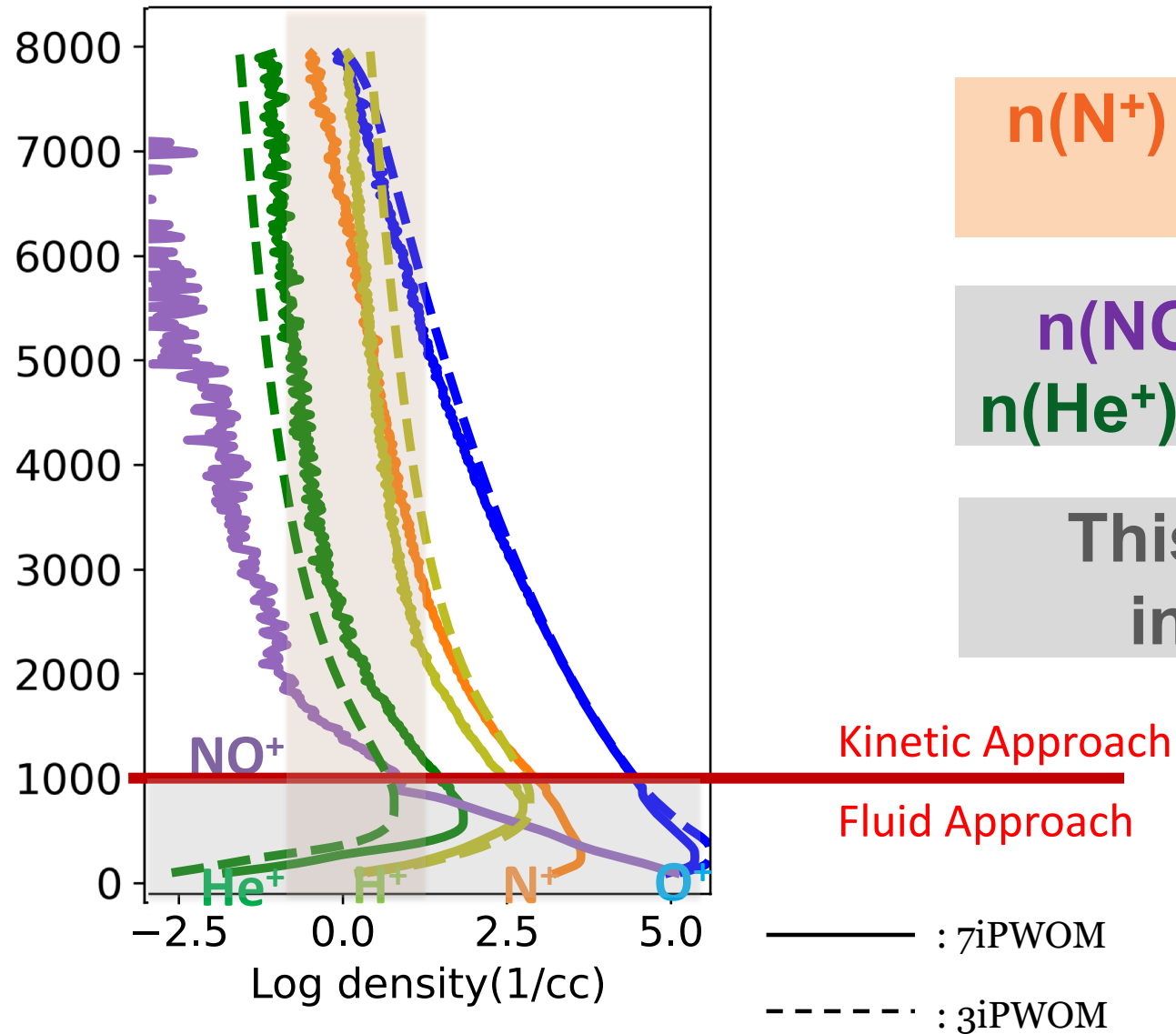
Steady State: 3iPWOM Fluid Solution



Steady State: 7iPWOM Fluid Solution (static NO^+)



7iPWOM Fluid + Kinetic Solution (Dynamic NO⁺)

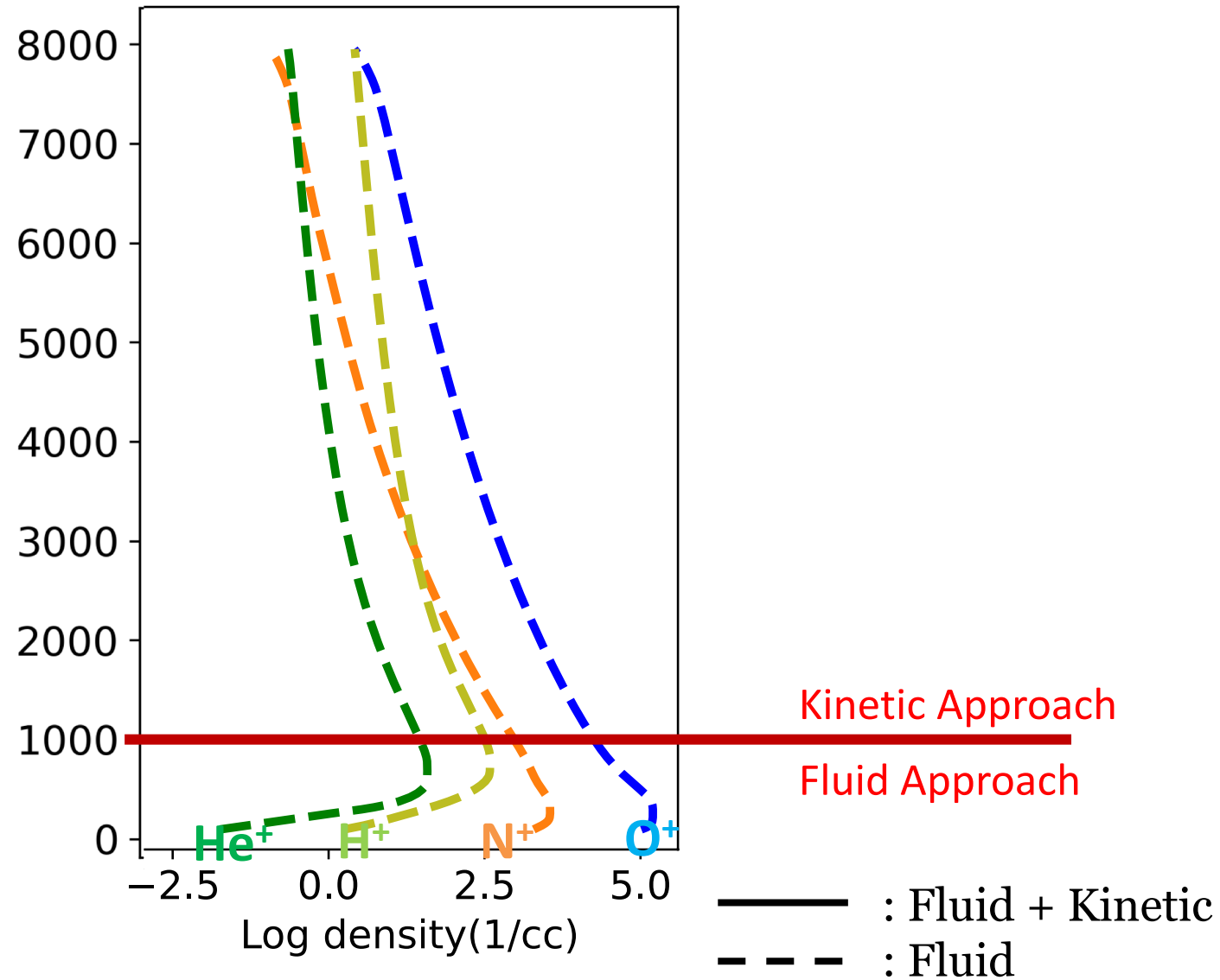


$n(\text{N}^+)$ is still important in the kinetic solution

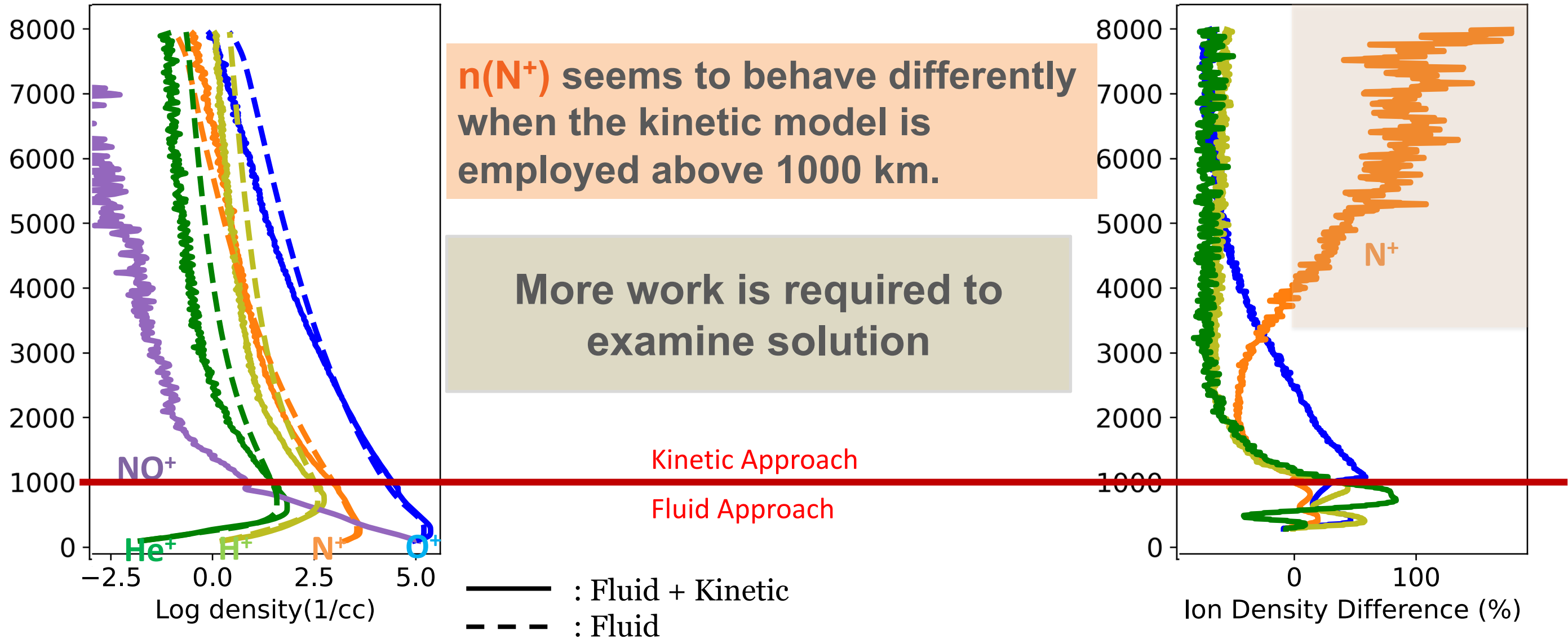
$n(\text{NO}^+)$ is comparable with $n(\text{He}^+)$ below 1000 km altitude

This simulation required increased resolution

Compare (Fluid + Kinetic) vs (Fluid) Solution



Compare (Fluid + Kinetic) vs (Fluid) Solution



Summary and Future work

- **N⁺ ions are a key species** in the ionosphere and their presence alter the outflow for all conditions.
- Comparison with **available data below 1200km**, 7iPWOM shows **tremendous improvement** of the outflow solution when N⁺ is included.
- Preliminary simulations using the kinetic 7iPWOM suggest that **molecular ions could also play an important role** in the local transport of all species [*more work to be done here*].
- The molecular ions, such as NO⁺, need to acquire sufficient energy in a very short time to escape from the ionosphere, and the energization of molecular ions, via wave particle interaction, are still under investigation.